

**3<sup>rd</sup> International Conference on  
Applied Mathematics & Approximation Theory  
May 28-31, 2015 – Ankara – Turkey**

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**AMAT 2015**

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**ABSTRACTS BOOK**

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**Venue: TOBB University of Economics and Technology  
Söğütözü Street No: 43, 06560 Ankara - Turkey**

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## Solution of Equation for Ruin Probability of Company for Some Risk Model by Monte Carlo Methods

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### Abstract

In classical risk model with Poisson damages stream that enter an insurance company with intensity's  $\lambda$  and accumulation speed of payments  $c$  and with damages distribution  $D(u)$  under condition  $\frac{\lambda b}{c} < 1$ , the equation is given as

$$R(x) = \frac{\lambda}{c} \int_0^x D(x-u)R(u)du + \frac{\lambda}{c} F(x),$$

where  $F(x) = \int_x^\infty D(t)dt$ ,  $b = \int_0^\infty t dD(t)$ ,  $R(x)$  stands for probability of ruin as a function of the initial capital  $x \geq 0$ . It is known that the function  $R(x)$  is monotone decreasing to 0 as  $x \rightarrow \infty$ . Proven fact that for continuous function  $F(x)$ ,  $x \geq 0$ , the integral equation for probability of ruin has continuous unique solution in  $C$  function class on interval  $[0, \infty)$ . This integral equation is not easy solved by "classical" methods when  $D(x)$  is Pareto distribution,  $D(x) \equiv P(x) = 0$ ,  $0 \leq u \leq \frac{\alpha-1}{\alpha}$ ;  $P(u) = 1 - \left(\frac{\alpha-1}{\alpha u}\right)^\alpha$ ,  $u > \frac{\alpha-1}{\alpha}$  with parameter  $\alpha = 3$ , with accuracy at most 0.03,  $\lambda = 0.7$ ,  $c = 1$ , for  $x > 500$ .

We solve this integral equation with any given accuracy for given parameters and for  $x > 500$  by Monte Carlo methods. The calculating experiment was realized for parameters  $\lambda = 0.8$ ,  $c = 1$ ,

$$F(x) = \begin{cases} 1, & \text{for } x \leq k, \\ \left(\frac{k}{x}\right)^\alpha, & \text{for } x > k \end{cases}$$

and also for Pareto distribution with parameters  $\alpha = 2, 3, 5, 7$  and  $k > 0$ ,  $k = \frac{\alpha-1}{\alpha}$ . Results of numerical experiments are completely satisfactory.

**Keywords:** Probability, ruin, model, integral equation, Pareto distribution, Monte Carlo methods.