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## Model free boundary problem for the parabolic equations with a small parameter

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Let  $D_1 = \{x \mid x' \in \mathbb{R}^{n-1}, x_n < 0\}$ ,  $D_2 = \{x \mid x' \in \mathbb{R}^{n-1}, x_n > 0\}$ ,  $D_T^{(m)} = D_m \times (0, T)$ ,  $m = 1, 2$ ,  $R_T = \{(x, t) \mid x' \in \mathbb{R}^{n-1}, x_n = 0, 0 < t < T\}$ . It is required to find functions  $u_1(x, t)$  and  $u_2(x, t)$  satisfying the conditions

$$\begin{aligned} \varepsilon \partial_t u_m - a_m \Delta u_m &= 0 \quad \text{in } D_T^{(m)}, \quad m = 1, 2, \\ u_m|_{t=0} &= 0 \quad \text{in } D_m, \quad m = 1, 2, \\ u_1 - u_2|_{R_T} &= 0, \quad b \nabla u_1 - c \nabla u_2|_{R_T} = \varphi(x', t), \end{aligned}$$

where  $b = (b_1, \dots, b_n)$ ,  $c = (c_1, \dots, c_n)$ , the coefficients  $a_m$ ,  $b_i$ ,  $c_i$ , ( $m = 1, 2$ ;  $i = 1, \dots, n$ ) are constants,  $\varepsilon > 0$  is a small parameter.

The problem are investigated in the Hölder space  $C^{1,1/2}(\bar{\Omega}_T)$  with the norm  $\|u\|_{C^{1,1/2}(\bar{\Omega}_T)}$ , and  $C_{x',t}^{1+\alpha, \frac{1+\alpha}{2}}(\bar{\Omega}_T)$  is a subset of functions  $u \in C_{x',t}^{1+\alpha, \frac{1+\alpha}{2}}(\bar{\Omega}_T)$  such that  $\frac{\partial^k u}{\partial t^k}|_{t=0} = 0$ ,  $k \leq [\frac{1+\alpha}{2}]$ .

**Theorem.** Let  $b_n > 0$ ,  $c_n > 0$ ,  $\varepsilon > 0$ . For every function  $\varphi(x', t) \in C_{x',t}^{1+\alpha, \frac{1+\alpha}{2}}(R_T)$ ,  $\alpha \in (0, 1)$ , the problem has a unique solution  $u_m \in C_{x',t}^{1+\alpha, \frac{1+\alpha}{2}}(D_T^{(m)})$ ,  $m = 1, 2$ , and this solution satisfies the estimate

$$\begin{aligned} \sum_{m=1}^2 \left\{ \|\partial_x^2 u_m\|_{x, D_T^{(m)}}^{(\alpha)} + \varepsilon^{\frac{1}{2}} \|\partial_x^2 u_m\|_{x, D_T^{(m)}}^{(\frac{\alpha}{2})} + \varepsilon \|\partial_t u_m\|_{x, D_T^{(m)}}^{(\alpha)} + \varepsilon^{1+\frac{\alpha}{2}} \|\partial_t u_m\|_{x, D_T^{(m)}}^{(\frac{\alpha}{2})} + \right. \\ \left. + \varepsilon^{\frac{1+\alpha}{2}} \|\partial_x u_m\|_{x, D_T^{(m)}}^{(\frac{1+\alpha}{2})} \right\} \leq C \left\{ \|\varphi\|_{R_T} + \varepsilon^{\frac{\alpha}{2}} \|\partial_{x'} \varphi\|_{R_T} + \varepsilon^{-\frac{1}{2}} \|\varphi\|_{R_T}^{(\frac{\alpha}{2})} \right\}, \end{aligned}$$

where the constant  $C$  does not depend on  $\varepsilon$ .

## Asymmetrical screw flows which minimize the integral remainder between the sides of the Boltzmann equation

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The Boltzmann equation for the model of hard spheres is considered. This non-linear kinetic integro-differential equation is the main instrument to study the complicated phenomena in the multiple-particle systems, in particular, rarefied gas. The well-known exact solutions of this equation in the form of global and local Maxwellians have been described so far only as equilibrium states of a gas. That is why the search of those or other approximate solutions is topical. This equation has form [1-2]:

$$D(f) = Q(f, f) \quad (1)$$