

STRONGLY COUPLED COULOMB SYSTEMS

FINAL PROGRAM  
& BOOK OF ABSTRACTS

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Kiel, July 30–August 4, 2017  
Wissenschaftszentrum Kiel

## Monday, July 31

**08:30 Opening**

### Session I: Dense and astrophysical plasmas

08:45	S. Mazevert	
[keynote]	<i>Ab initio equation of states for planetary and exoplanetary modeling</i>	24
09:30	V.K. Gryaznov <i>Thermodynamics of deuterium at terapascal pressure range</i>	25
09:45	M. Schöttler <i>Miscibility gap of hydrogen-helium mixtures</i>	26
10:00	V. Mintsev <i>The possibilities of proton radiography for the strongly coupled plasma EOS measurements</i>	27

**10:15 Coffee break and informal discussions**

### Session II: Classical charged particle systems

10:45	M. Manghi	
[invited]	<i>Ionic transport through hydrophobic nanopores: theory and experiments</i>	28
11:15	E. Allahyarov <i>The role of Coulomb correlations in nano-composite materials with high-k inclusions</i>	29
11:30	Y. Feng <i>Experiments and simulations on dusty plasmas</i>	30
12:00	E. Kostadinova <i>Transport properties of a disordered 2D complex plasma crystal</i>	31
12:15	W. Schröer <i>Critical and non-critical fluctuations in mixtures of ionic liquids with alcohols in the vicinity of the liquid-liquid phase transition</i>	32

**12:30 Lunch and informal discussions**

### Session III: Dynamics of correlated quantum Coulomb systems

14:30	S. Kuhr	
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15:15	N. Schlünzen <i>Ab initio simulations of the transport of strongly correlated fermions</i>	34
15:45	B. He <i>Simulation of stopping power and evolution of ion temperature in plasmas</i>	35
16:00	S. Tanaka <i>Constructing the free energy of finite-temperature spin-polarized electron liquids from quantum many-body theories</i>	36

**16:15 Coffee break and informal discussions**

### Poster introductions and poster session I

**16:30–18:00**

## Tuesday, August 1

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09:15	J. Dai	
	<i>Interplay between quantum electrons and coupled ions: ion-electron temperature relaxation in dense hydrogen</i>	38
09:30	C. Lin	
	<i>Ionization potential depression in terms of the dynamical structure factor</i>	39
09:45	A.S. Shumikhin	
	<i>Equation of state and transport properties of metals in warm dense matter regime</i>	40
10:00	Y. Hou	
	<i>Influence of the ionization on ionic transport properties in the warm dense regime</i>	41

### 10:15 Coffee break and informal discussions

### Session V: Confined and mesoscopic Coulomb systems

10:45	G. Baym	
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	<i>Excitonic condensation and quadriexcitons in a symmetric electron-hole bilayer with valley degeneracy: QMC simulations</i>	43
11:45	Yu.E. Lozovik	
[invited]	<i>Strongly correlated electron-hole 2D systems: current status and perspectives</i>	44
12:15	I.Ya. Polishchuk	
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### 12:30 Lunch and informal discussions, IAB meeting

### Session IV: Dynamics of correlated quantum Coulomb systems

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15:00	Z. Jurek	
	<i>Simulations of high intensity x-ray generated plasmas</i>	47
15:15	C. Dharma-wardana	
	<i>Phase transitions in low-Z warm-dense-matter Carbon systems; NPA-DFT predictions of EOS, conductivity and XRTS spectra</i>	48
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### 16:15 Coffee break and informal discussions

**Poster introductions and poster session II**

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10:15 Coffee break and informal discussions

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	<i>Coupled plasmon modes in vertically stacked 2D nanomaterials</i>	58
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12:30 Lunch and informal discussions

### Conference excursion to Lübeck

14:00–20:00

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#### 10:30 Coffee break and informal discussions

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#### 12:30 Lunch and informal discussions

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#### 16:15 Coffee break and informal discussions

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### Conference dinner

19:30–23:00

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# Direct determination of dynamic properties of strongly coupled plasmas

I.M. Tkachenko<sup>\*1</sup>, Yu.V. Arkhipov<sup>2</sup>, A.B. Ashikbayeva<sup>2</sup>, A. Askaruly<sup>2</sup>, L. Conde<sup>3</sup>,  
 A.E. Davletov<sup>2</sup>, Z. Donkó<sup>4</sup>, D.Yu. Dubovtsev<sup>2</sup>, P. Hartmann<sup>4</sup>, I. Korolov<sup>4</sup>,  
 S. Syzganbayeva<sup>2</sup>

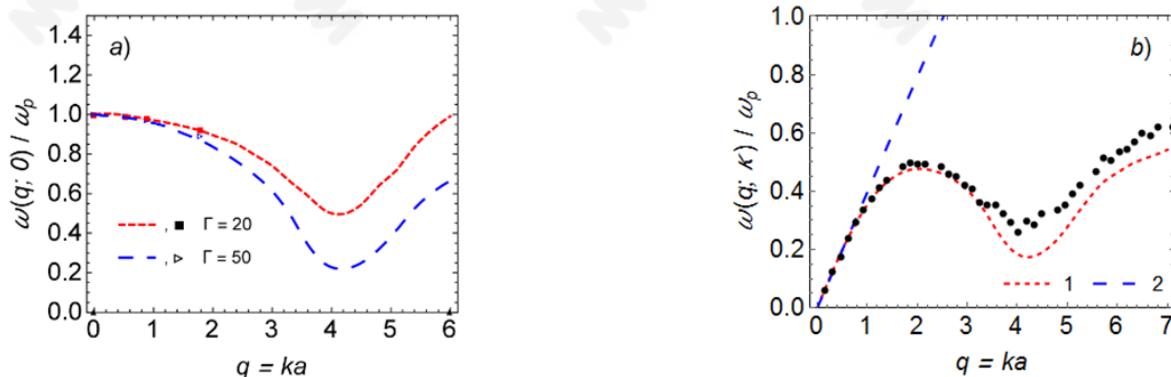
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A closed algorithm is suggested which allows the determination of dynamic characteristics of various strongly coupled plasmas (one- and two-component plasmas, electron gas, etc.) within the non-perturbative model-free moment approach without any data input from simulations or direct experiments. The standard Nevanlinna formula (see [1,2] and references therein) for the loss function (LF) which incorporates its independently calculated power frequency moments or the sum rules is complemented with an observation with respect to the LF low-frequency behavior [2]. Thus, the constructed LF satisfies all involved sum rules automatically and permits to determine the system's dynamic structure factor (DSF), the dispersion, the decay, and other characteristics of the collective modes using only the (partial) static structure factors obtained numerically or theoretically. For one-component plasmas it also provides a model for the dynamic local-field correction [3]. Simplified interpolation formulas for the LF moments, which do not need the external static data, are also suggested whose validity confirms the robustness of the present approach. A good quantitative agreement with molecular dynamics simulation data is achieved in a wide realm of variation of the system parameters, see, for example, the following figures where our results computed on the basis of static characteristics obtained by the molecular-dynamics (MD) method are compared to the MD dynamic data.



**Figure:** Dispersion of plasma modes compared to MD data (figures): a) Coulomb OCP, b) Yukawa OCP at  $\Gamma=100$  and  $\kappa=2$ . Line 2 stands for the sound mode.  $a$  is the Wigner-Seitz radius.

[1] I. M. Tkachenko, Y. V. Arkhipov, and A. Askaruly, *The Method of Moments and its Applications in Plasma Physics* (Lambert, Saarbrücken, 2012)

[2] Yu. V. Arkhipov et al., Phys. Rev. E **90**, 053102 (2014), *ibid*, **91**, 019903 (2015)

[3] Yu.V. Arkhipov et al., Phys. Rev. E **81**, 026402 (2010)

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# Two-component plasma stopping power directly from partial static structure factors

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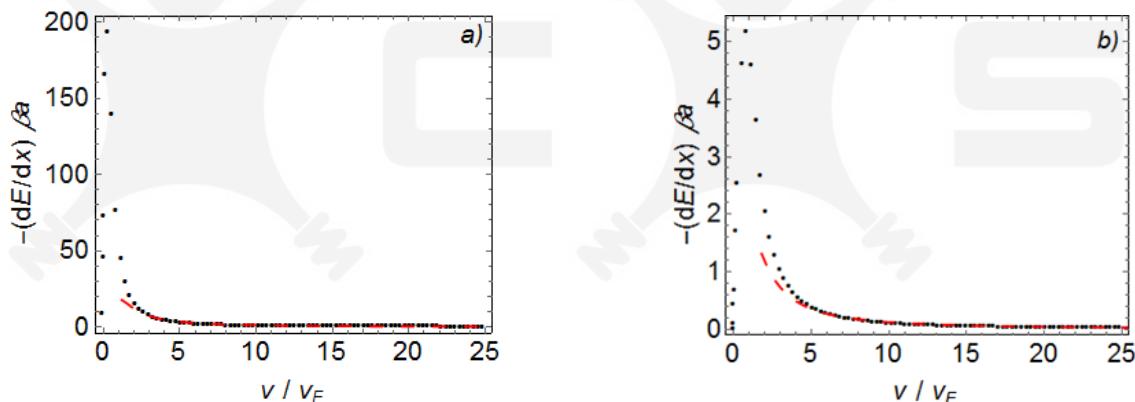
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Reliable knowledge of energy losses of heavy projectiles is of substantial significance for the progress of inertial fusion and other practical applications. Polarizational stopping power of hydrogen-like dense plasmas

$$\left[ -\frac{dE}{dx} \right]^{pol} = \frac{2(Z_p e)^2}{\pi v^2} \int_0^\infty \frac{dk}{k} \int_0^{kv} \omega^2 L(k, \omega) d\omega,$$

( $Z_p e$  and  $v$  are the projectile charge and velocity) is studied within the moment approach which constructs the system loss function,  $\varepsilon(k, \omega)$  being the system dielectric function, in terms of only the system partial static structure factors so that  $L(k, \omega)$  satisfies all convergent sum rules and other exact relations [1,2]. Electron-ion correlations in the target plasma are also taken into account [3] without using the simulation data. Enhancement of the stopping power is observed with respect to that in electron fluids [4], where the asymptotic values are always higher than the calculated ones, see Figure, for example.



**Figure:** Calculated stopping power (dots) and its asymptotic form (red dashed line) [3] at a)  $\Gamma = \beta e^2/a = 10.77$ ; b)  $\Gamma = 1.077$ ,  $\beta^{-1}$ ,  $a$ , and  $v_F$  are the plasma temperature, electronic Wigner-Seitz radius and Fermi velocity, respectively. The structure factors were calculated in the hyper-netted chain approximation.

- [1] I. M. Tkachenko, Y. V. Arkhipov, and A. Askaruly, *The Method of Moments and its Applications in Plasma Physics* (Lambert, Saarbrücken, 2012) and references therein
- [2] I. M. Tkachenko et al., To be presented at the SCCS 17 Conference
- [3] D. Ballester, I. M. Tkachenko, Phys. Rev. Lett., **101**, 075002, (2008)
- [4] M.D. Barriga-Carrasco, D. Casas, R.S. Morales, Phys. Rev. E, **93**, 033204, (2016) and references therein

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# Calculating structural characteristics of one-component plasmas

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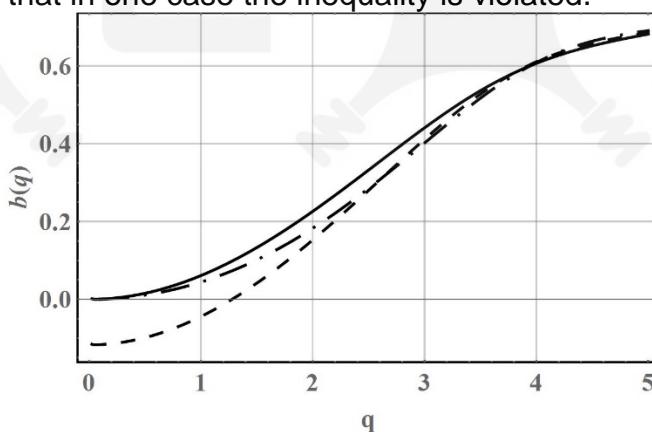
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Practical application of research results on one-component plasma has found its reflection in various areas, such as astrophysics, lithography, dusty plasmas, ultracold plasmas, etc. Therefore, study of static and dynamic properties of OCP is of significant importance.

There is a number of theoretical methods of calculation of the static characteristics based on integral equations, fitting approximations and empirical formulas with the results of simulations often taken as reference. In this case, it is traditionally accepted that the theoretical results should be in a good agreement with the latter.

Not all of the above theoretical methods can be employed to calculate dynamic characteristics by the method of moments [1]. In the present work, we propose to qualify the static characteristics through the Hölder or Cauchy-Schwarz inequalities for the application of the above methods,  $b>0$ . The function  $b$  depends on the plasma thermodynamic characteristics via the static structure factor.

Precisely, we consider the hyper-netted chain (HNC) approximation with and without the empirical bridge function proposed by Ng [2], the modified HNC approximation (MHNC) [3], the variational modified HNC (VMHNC) [4], and other empirical and fitting formulas, e.g., [5]. For example, in Figure we present data for the HNC and the VMHNC, and show that in one case the inequality is violated.



**Figure:** Criterion of satisfaction of the Cauchy-Schwarz inequality,  $b>0$ , at  $\Gamma=16$  for various theoretical methods: HNC (solid line); HNC with the bridge function [2] (dashed line); VMHNC [4] (dot dashed line).

- [1] I. M. Tkachenko et al., The present Conference
- [2] K.-Ch. Ng, J. Chem. Phys. **61**, 2680 (1974)
- [3] G. Faussurier. M. S. Murillo, Phys. Rev. E. **67**. 046404 (2003).
- [4] G. Faussurier. Phys. Rev. E **69**, 066402 (2004)
- [5] N. Desbiens. P. Arnault. J. Clérouin. Physics of Plasma. **23**. 092120 (2016).

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