

# **RE: ASMDA 2015: abstract submission**

1 message

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On ordered categorical modelling for complex skill development

Pya, N.Y , Kussainov, A.S.

Dear Dr. Natalya Pya,

We are happy to inform you that according to the Conference Committee decision your Abstract submitted to the 16th ASMDA 2015 International Conference (June 30 - July 4, 2015, University of Piraeus, Greece) was accepted for an oral presentation. Thank you.

Sincerely yours, The Conference Secretariat

-----Original Message-----From: Natalya Pya [mailto:n.y.pya@bath.ac.uk] Sent: Friday, September 26, 2014 2:27 PM To: secretariat@asmda2015.com Cc: arman.kussainov@gmail.com; Natalya Pya Subject: ASMDA 2015: abstract submission

Dear Sir/Madam,

With this email I would like to submit an abstract for a presentation at a Contributed session of the ASMDA 2015 conference.

Thank you for your time and consideration in advance.

Kind regards, Natalya

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Dr Natalya Pya, Research Associate Department of Mathematical Sciences, University of Bath, Claverton Down Bath BA2 7AY, UK Thu, Oct 9, 2014 at 3:38 AM

# On ordered categorical modelling for complex skill development

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**Abstract.** In cognitive science there has been considerable interest in the understanding of expertise development. Models for exploring human complex skill development are often based on comparisons between experts and novices, and use measurements of performance at different levels of skills as predictors. In this paper we study the development of expertise by analysing video game telemetry data collected from a real-time strategy game. Data that relate to cognitive-motor abilities, attentional and perceptual processes were collected from StarCraft 2 game players from seven levels of expertise. We develop an extended generalized additive model for ordered categorical data to investigate the effects of predictors on skill development. **Keywords:** ordered categorical, cognitive science, generalized additive models, skill learning.

# 1 Introduction

Thompson *et al.*[18] conducted a study exploring human complex skill development. Their aim was to identify potential predictors of expertise in real-time strategy (RTS) video games using the telemetric data collected from RTS StarCraft 2 game players. StarCraft 2 is a popular video game which has millions of players worldwide. Thompson *et al.*[18] examined measures that relate to cognitive-motor abilities, attentional and perceptual processes. Using random forest classifiers, they disproved the assumption that importance of variables across skill levels remains static. Moreover, they argue that telemetric data can become a standard tool for studying human cognition and learning. As different expert areas such as, e.g. chess, basketball, surgery, are expected to show sufficient consistency in development of expertise, many studies have been devoted to exploring skill development in strategy games (Chase and Simon[8], Charness[9], Ericsson and Charness[10]).

This paper proposes to investigate development of expertise using additive regression modelling. The paper develops an extended generalized additive model for ordered categorical data (Wood *et al.*[19]) to study the effects of predictors on skill learning. Modelling categorical responses using smooth functions of predictors allows us to confirm Thompson *et al.*[18] findings and to further investigate the effects of predictors on skill development.

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### 2 Video game data

The telemetric data collected from 3,360 RTS StarCraft 2 game players from 7 levels of expertise. The dataset is public available at UCI Machine Learning Repository (Bache and Lichman[5]). For each player, the level of expertise measured by the league in which they contend, serves as an ordered response  $Y_i$ .  $Y_i$  takes a value from r = 1, 2, ..., 7, indicating Bronze, Silver, Gold, Platinum, Diamond, Master, and Professional leagues. There are eighteen predictor variables available including measures of attentional control, perceptual process and cognitive-motor speed. The examination of the data and preliminary modelling revealed 13 variables relevant to skill development. Table 1 summarizes the predictors under study. The time at which values of the predictors is recorded is in terms of timestamps in the StarCraft 2 replay file. GapBwPACs, ActionLatency, NumberOfPACs, and ActionsInPAC are four variables that refer to a certain period of time during which a player performs at a specific location. Perception action cycle (PAC) was defined by Thompson *et al.*[18] as screen fixations with one or more actions. For the complete information about the variables used in the study, see Thompson *et al.*[18].

Name	Description	Min	Max
APM	Action per minute	22.06	389.83
SelectByHotkeys	Number of unit or building selections	0	0.043
	made using hotkeys per timestamp		
AssignToHotkeys	Number of units or buildings assigned	0	$1.75 \cdot 10^{-3}$
	to hotkeys per timestamp		
UniqueHotkeys	Number of unique hotkeys used per	0	10
	timestamp		
MinimapAttacks	Number of attack actions on minimap	0	$3.02 \cdot 10^{-3}$
	per timestamp		
NumberOfPACs	Number of perception action cycles (PAC)	$6.79 \cdot 10^{-4}$	$7.97 \cdot 10^{-3}$
	per timestamp		
GapBwPACs	Mean duration in milliseconds between	6.667	237.143
	PACs		
ActionLatency	Mean latency from the onset of PACs	24.09	176.37
	to their first action in milliseconds		
ActionsInPAC	Mean number of actions within each PAC	2.039	18.558
TotalMapExplored	The number of 24x24 game coordinate	5	58
	grids viewed by the player per timestamp		
WorkersMade	Number of SCVs, drones, and probes	$7.7 \cdot 10^{-5}$	$5.15 \cdot 10^{-3}$
	trained per timestamp		
UniqueUnitsMade	Unique unites made per timestamp	2	13
ComplexAbilUsed	Abilities requiring specific targeting	0	$3.08 \cdot 10^{-3}$
	instructions used per timestamp		

Table 1. Telemetric data characteristics

#### **3** Modelling approach

Many models have been proposed to analyze ordered categorical data which became well-known by virtue of Cox[7] and Plackett[16]. The most appealing regression models for ordered categories are cumulative logit (proportional-odds version of the cumulative logit) models expressed in terms of a latent usually unobservable continuous variable proposed by McCullagh[15], Anderson and Philips[4], Hastie and Tibshirani[13]. McCullagh[15] and Anderson and Philips[4] introduced parametric regression models with ordered categorical responses, whereas Hastie and Tibshirani[13] extended this to a non-parametric version. The parameter estimation for those models is based on maximizing likelihood assuming independent multinomial observations using Fisher scoring algorithm. The cumulative logit models were also discussed in Anderson[3], Agresti[1], Agresti[2], Goodman[12]. Fahrmeir and Lang[11], Kneib and Fahrmeir[14] developed a general class of semi-parametric additive regression models for categorical responses from a Bayesian perspective.

#### Extended generalized additive model

The model proposed in this paper is within a new general framework to generalized additive modelling for non-exponential family responses introduced by Wood et al.[19]. The framework of Wood et al.[19] proposes two methods for the generalized additive models (GAM) generalization: an extended GAM fitting for the cases with a single linear predictor and a log likelihood expressed as a sum over the log likelihood for each response datum; and a general model estimation when log likelihood depends non-linearly on smooth functions of predictors. The first method includes such distributions outside the exponential family as beta, zero inflated Poisson, negative binomial, Tweedie, scaled t distribution and ordered categorical data. The GAM fitting method is extended for these models. The second extension requires different approach for model fitting and general and reliable smoothing parameter estimation. It covers such models as Cox proportional hazard (Cox[6]) and Cox process models, generalized additive models for location scale and shape proposed by Rigby and Stasinopoulos[17] and multivariate additive models (Yee and Wild[21]). Below is a brief description of modelling with ordered categorical responses within a new extended GAM.

Consider independent response observations,  $y_i$ , that take values from r = 1, ..., R, where r is ordered category label. A latent variable  $u_i = \mu_i + \epsilon_i$  is introduced with the c.d.f. of  $\epsilon_i$  being F. Then, given  $-\infty = \alpha_0 < \alpha_1 < ... < \alpha_R = \infty$ ,  $y_i = r$  if a latent variable  $u_i$  is such that  $\alpha_{r-1} < u_i \leq \alpha_r$ ,

$$P(Y_{i} = r) = F(\alpha_{r} - \mu_{i}) - F(\alpha_{r-1} - \mu_{i}).$$

The usual choice for the c.d.f. of  $\epsilon$  is the standard logistic or normal. For identifiability reasons  $\alpha_1 = -1$ , so there are R - 2 extra unknown parameters. To impose increasing ordering on the cutting points,  $\alpha_r$  are set as

$$\alpha_r = \alpha_1 + \sum_{j=1}^{r-1} \exp(\theta_j), \quad 1 < r < R,$$

so  $\theta_j$  are parameters to be estimated. The mean value of the latent variable depends on the predictor variable in the following way,

$$\mu_i = \mathbf{A}_i \boldsymbol{\gamma} + \sum_j f_j(x_{ji}),$$

where **A** is a model matrix for the strictly parametric terms,  $\gamma$  is a vector of unknown parameters,  $f_j$  is an unknown smooth function of the predictor variable  $x_j$ , where  $x_j$  can be vector valued. Each smooth term is represented by reduced rank spline smoothers  $f_j(x_j) = \sum_k \beta_{kj} b_{kj}(x_j)$ , where  $b_{kj}$  are known spline basis functions,  $\beta_{kj}$ unknown coefficients. Then, the mean of the latent variable can be expressed as  $\mu = \mathbf{X}\beta$ , with the model matrix **X** combining **A** and matrix of spline basis, and  $\gamma$  being a part of  $\beta$ .

The log likelihood of the model can be written as

$$l = \sum_{i=1}^{n} l_i(y_i, \mu_i, \boldsymbol{\theta}),$$

where  $l_i$  is the log likelihood for each observation,  $\boldsymbol{\theta}$  is a (R-2)-vector of the extra parameters,  $\theta_j$ , that control the thresholds. Then, the deviance corresponding to the observation  $y_i$  is defined in the standard way as  $D_i = 2(\tilde{l}_i - l_i)$ , where  $l_i = \max_{\mu_i} l_i(y_i, \mu_i, \boldsymbol{\theta})$  is the saturated log likelihood. Given  $\boldsymbol{\theta}$ , the parameters  $\boldsymbol{\beta}$  are estimated by minimization of the penalized deviance

$$\mathcal{D}(oldsymbol{eta},oldsymbol{ heta}) = \sum_i D_i(oldsymbol{eta},oldsymbol{ heta}) + \sum_j \lambda_j oldsymbol{eta}^T \mathbf{S}^j oldsymbol{eta},$$

where a quadratic penalty term  $\beta^T \mathbf{S}^j \beta$  measuring function smoothness is associated with each smooth  $f_j$  and  $\lambda_j$  being a smoothing parameter. Penalized iteratively re-weighted least squares (PIRLS) is applied for  $\beta$  estimation. Estimation of  $\theta$  is achieved by minimization of the negative Laplace approximate marginal likelihood (LAML),

$$\mathcal{V} = \frac{\mathcal{D}(\hat{\boldsymbol{\beta}}, \boldsymbol{\theta})}{2} - \tilde{l}(\boldsymbol{\theta}) + \frac{\log |\mathbf{X}^T \mathbf{W} \mathbf{X} + \mathbf{S}^{\lambda}| - \log |\mathbf{S}^{\lambda}|_+}{2} - \frac{M_p}{2} \log(2\pi),$$

where  $\mathbf{S}^{\lambda} = \sum_{j} \lambda_{j} \mathbf{S}^{j}$  and  $|\mathbf{S}^{\lambda}|_{+}$  is the product of the positive eigenvalues of  $\mathbf{S}^{\lambda}$ ,  $M_{p}$  is the number of zero eigenvalues of  $\mathbf{S}^{\lambda}$ . Newton's or a quasi-Newton's method is used for  $\mathcal{V}$  minimization. Several issues with numerical instability have to be taken into account to make the optimization procedure efficient and reliable. This is fully covered in Wood *et al.*[19]. Generalized additive modelling with ordered categorical data as well as other extensions are implemented in an R package mgcv available at CRAN (Wood[20]).

#### Additive model for video game data

The preliminary backward selection, first in the framework of a generalized linear model and then in the framework of an extended GAM, revealed thirteen covariates

relevant to skill development (see section 2). The extended GAM for ordered categorical data with R = 7 was fitted with the selected set of predictors using smooth terms. We first consider a model with all selected predictors having non-linear effects on the mean of the ordered categorical latent variable.

Model 1:

$$\begin{split} \mu_i &= f_1(\texttt{NumberOfPACs}_i) + f_2(\texttt{UniqueHotkeys}_i) + f_3(\texttt{WorkersMade}_i) \\ &+ f_4(\texttt{GapBwPACs}_i) + f_5(\texttt{ActionLatency}_i) + f_6(\texttt{AssignToHotkeys}_i) \\ &+ f_7(\texttt{MinimapAttacks}_i) + f_8(\texttt{APM}_i) + f_9(\texttt{SelectByHotkeys}_i) \\ &+ f_{10}(\texttt{ActionsInPAC}_i) + f_{11}(\texttt{TotalMapExplored}_i) \\ &+ f_{12}(\texttt{UniqueUnitsMade}_i) + f_{13}(\texttt{ComplexAbilUsed}_i), \end{split}$$

where the model terms  $f_1 - f_{13}$  are unknown smooth functions of the corresponding predictors. Thin plate regression splines are used for their representations. The predictor values were preprocessed using square root or log transformation in order to avoid gaps with very small amount of data that account for the Professional league. There was a significant linear dependence of NumberOfPACs, UniqueHotkeys and WorkersMade on the mean of the latent variable, so that it was sufficient to add strictly parametric structure for these three predictors. The resulted model has the following structure.

Model 2:

$$\begin{split} \mu_i &= \beta_1 \cdot \text{NumberOfPACs}_i + \beta_2 \cdot \text{UniqueHotkeys}_i + \beta_3 \cdot \text{WorkersMade}_i \\ &+ f_1(\text{GapBwPACs}_i) + f_2(\text{ActionLatency}_i) + f_3(\text{AssignToHotkeys}_i) \\ &+ f_4(\text{MinimapAttacks}_i) + f_5(\text{APM}_i) + f_6(\text{SelectByHotkeys}_i) \\ &+ f_7(\text{ActionsInPAC}_i) + f_8(\text{TotalMapExplored}_i) \\ &+ f_9(\text{UniqueUnitsMade}_i) + f_{10}(\text{ComplexAbilUsed}_i), \end{split}$$

where  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  are unknown parameters.

Including the bivariate smooth of the APM and the second most important variable, SelectByHotkeys, gives better model in comparison with the model with univariate effect of the APM. Moreover, constructing a tensor product interaction of GapBwPACs and ActionLatency, with their main effects being included separately further improves the model fit. The following additive structure for the mean value of the ordered categorical latent variable was considered as the third model.

Model 3:

$$\begin{split} \mu_i &= \beta_1 \cdot \texttt{NumberOfPACs}_i + \beta_2 \cdot \texttt{UniqueHotkeys}_i + \beta_3 \cdot \texttt{WorkersMade}_i \\ &+ f_1(\texttt{GapBwPACs}_i) + f_2(\texttt{ActionLatency}_i) \\ &+ f_3(\texttt{GapBwPACs}_i,\texttt{ActionLatency}_i) + f_4(\texttt{AssignToHotkeys}_i) \\ &+ f_5(\texttt{MinimapAttacks}_i) + f_6(\texttt{APM}_i,\texttt{SelectByHotkeys}_i) \\ &+ f_7(\texttt{ActionsInPAC}_i) + f_8(\texttt{TotalMapExplored}_i) \\ &+ f_9(\texttt{UniqueUnitsMade}_i) + f_{10}(\texttt{ComplexAbilUsed}_i), \end{split}$$

where all the predictors except for the first three have nonparametric smooth effects. A tensor product interaction of GapBwPACs and ActionLatency, is used for representing  $f_3$  with the main effects comprised in  $f_1$  and  $f_2$ .

# 4 Results and discussion

In addition to the above mentioned models, we fitted submodels with certain terms omitted. The model selection procedure showed that the best model in terms of the Akaike information criterion is the full model 3. Other model performance measures such as generalized cross validation score, adjusted  $r^2$  and percentage deviance explained were also better for model 3 than for other considered models.

Figure 1 illustrates the estimated effects of the two bivariate smooths of model 3. APM variable is used as a measure of cognitive speed. This variable is shown to have the highest rank of the predictive importance Thompson *et al.*([18]) in distinguishing Bronze-Professional classifier. The first decreasing trend of the APM (figure 1, right panel) is due to the high correlation between the APM and SelectByHotkeys variables (higher values of the covariate effect correspond to higher league level). Both predictors have increasing trends when considered separately as smooths of a single variable.



**Fig. 1.** Video game data: the estimated interactions between Gap Between PACs and Action Latency variables, and between APM and Select By Hotkeys.

The estimates of the univariate effects are shown in figure 2. As expected, the main effects of the two characteristics of the PACs, GapBwPACs and ActionLatency, are decreasing with increase in the skill level (panels (a) and (b)), while the other two have increasing trends (panel (e) and the positive parametric effect of NumberOfPACs). An adaptive smoother was used to estimate the effect of the ActionsInPAC, that allowed the degree of smoothing to vary along the range of the predictor values.



Fig. 2. Video game data: the estimated univariate smooth effects.

The strong increasing effect of the MinimapAttacks (fig. 2, panel (d)) which is used as a measure of the attentional control, supports the hypothesis of Thompson *et al.*[18] that more skillful players act on minimap more often. On the contrary the TotalMapExplored has a decreasing trend (panel (f)), more skillful players view the total map less often. Usage of hotkeys allows players to build and control game units in more efficient way, so that the higher values of the AssignToHotkeys variable would correspond to higher level of expertise (panel (c)). The estimated effects of the last two predictors do not have such monotonic features as for the other smooths. Players in the highest leagues seem to use moderately abilities that require particular targeting instructions (panel (h)), and keeping from the production of the Unique Units (panel (g)). Whereas, the lowest league players make medium number of units while avoiding complex abilities. The estimated monotone increasing trend of the WorkersMade shows that to progress players must produce more workers. However, the importance of this variable diminishes for the highest league (Thompson *et al.*[18]), which is explained by possible automatization of the worker production skill. Moreover, to advance in skills, players are required to put more effort on managing their learning and increasing cognitive demand, which is reflected by the positive linear trend of the UniqueHotKeys predictor.

This study supports Thompson's *et al.* [18] proposition that telemetric data can be used as a standard tool for studying human cognition and learning. Moreover, the proposed model confirms the previous findings that the assumption that importance of predictors across skill levels remains static is not correct. We showed that constructing non-isotropic tensor product splines used to model smooth interactions improves prediction of skill development. Modelling categorical responses using smooth functions of predictors allows to capture skill learning in a continuous fashion.

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