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# Winds of Stars and Exoplanets

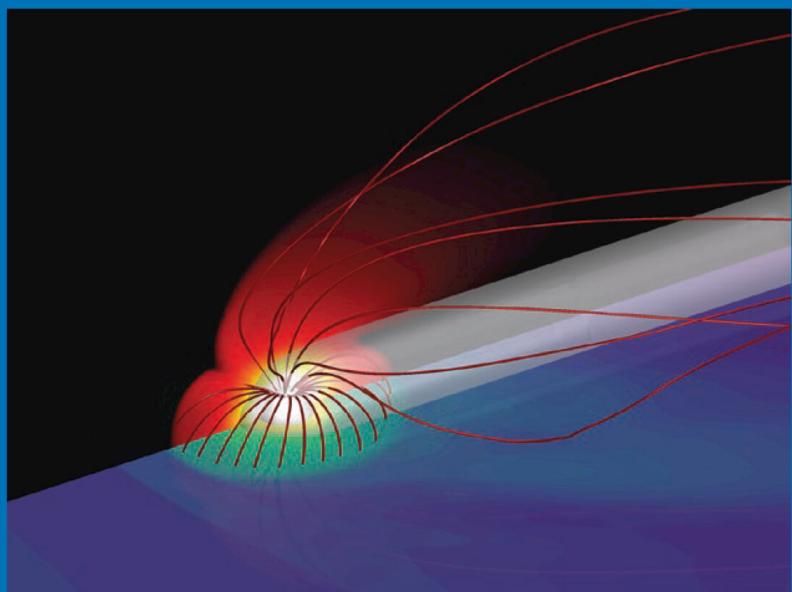
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*COVER ILLUSTRATION:*

Three-dimensional simulation of the escaping atmosphere of a close-in exoplanet interacting with the wind of its host star. The red field lines represent the planetary magnetic field, while the contours represent the total density (horizontal plane) and the neutral hydrogen density (vertical plane). Figure from Carolan et al 2021.

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# Evolution equations of the multi-planetary problem with variable masses

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**Abstract.** We investigated the influence of the variability of the masses of planets and the parent star on the dynamic evolution of  $n$  planetary systems, considering that the masses of bodies change isotropically with different rates. The methods of canonical perturbation theory, which developed on the basis of aperiodic motion over a quasi-conical cross section and methods of computer algebra were used.  $4n$  evolutionary equations were obtained in analogues of Poincare elements. As an example, the evolutionary equations of the three-planet exosystem  $K2 - 3$  were obtained explicitly, which is a system of 12 linear non-autonomous differential equations. Further, the evolutionary equations will be investigated numerically.

**Keywords.** celestial mechanics, variable mass, analogues of Poincare elements, multi-planetary system, secular perturbation.

## 1. Introduction

To date, there are more than 5,000 confirmed exoplanets and more than 3,800 planetary systems in the [NASA \(2022\)](#) database. To research exoplanetary systems in the non-stationary stage of their evolution is represented important interest.

## 2. Problem statement

We considered the problem of  $n + 1$  bodies with variable masses  $m_0 = m_0(t)$  – mass of the parent star  $S$ ,  $m_i = m_i(t)$ , – the mass of the planet  $P_i$ . The laws of mass are known and given functions of time  $m_0 = m_0(t)$ ,  $m_1 = m_1(t), \dots, m_n = m_n(t)$ , ( $n \geq 3$ ). The masses of spherical symmetric bodies change isotropically with different rates  $\dot{m}_0/m_0 \neq \dot{m}_i/m_i$ ,  $\dot{m}_i/m_i \neq \dot{m}_j/m_j$   $i, j = 1, 2, \dots, n$ ,  $i \neq j$ .

Differential equations of motion of  $n$  bodies with isotropically varying masses in a relative coordinate system are given in [Minglibaev \(2012\)](#)

$$\ddot{\vec{r}}_i = -f \frac{(m_0 + m_i)}{r_i^3} \vec{r}_i + f \sum_{j=1}^n {}' m_j \left( \frac{\vec{r}_j - \vec{r}_i}{r_{ij}^3} - \frac{\vec{r}_j}{r_j^3} \right), \quad (i, j = 1, 2, \dots, n), \quad (2.1)$$

where  $r_{ij} = r_{ji} = \sqrt{(x_j - x_i)^2 + (y_j - y_i)^2 + (z_j - z_i)^2}$  – mutual distances of the center of spherical bodies,  $f$  – gravitational constant,  $\vec{r}_i(x_i, y_i, z_i)$  – the radius-vector of center of the planet  $P_i$ , the sign "stroke" when summing means that  $i \neq j$ .

For our purposes, analogues of the second system of canonical Poincare elements are preferred

$$\Lambda_i, \lambda_i, \xi_i, \eta_i, p_i, q_i, \quad (2.2)$$

which are introduced on the basis of elements of aperiodic motion over a quasi-conical cross section [Minglibaev \(2012\)](#)

### 35 3. Evolutionary equations of $n$ planets with variable masses

36 The evolutionary equations of  $n$  planets with variable masses in dimensionless variables  
 37 (2.2)-(2.5) in the non-resonant case have the form in our work Prokopenya et al. (2022)

$$\xi'_i = \sum_{s=1}^{i-1} m_s \left( \frac{\Pi_{ii}^{is}}{\Lambda_i} \eta_i + \frac{\Pi_{is}^{is}}{\sqrt{\Lambda_i \Lambda_s}} \eta_s \right) + \sum_{k=i+1}^n m_k \left( \frac{\Pi_{kk}^{ik}}{\Lambda_i} \eta_i + \frac{\Pi_{ik}^{ik}}{\sqrt{\Lambda_i \Lambda_k}} \eta_k \right) - \frac{3\gamma_i''}{2\gamma_i} \frac{\Lambda_i^3}{\mu_{i0}^2} \eta_i, \quad (3.1)$$

$$\eta'_i = - \sum_{s=1}^{i-1} m_s \left( \frac{\Pi_{ii}^{is}}{\Lambda_i} \xi_i + \frac{\Pi_{is}^{is}}{\sqrt{\Lambda_i \Lambda_s}} \xi_s \right) - \sum_{k=i+1}^n m_k \left( \frac{\Pi_{kk}^{ik}}{\Lambda_i} \xi_i + \frac{\Pi_{ik}^{ik}}{\sqrt{\Lambda_i \Lambda_k}} \xi_k \right) + \frac{3\gamma_i''}{2\gamma_i} \frac{\Lambda_i^3}{\mu_{i0}^2} \xi_i, \quad (3.2)$$

$$p'_i = - \sum_{s=1}^{i-1} m_s B_1^{is} \left( \frac{q_i}{4\Lambda_i} - \frac{q_s}{4\sqrt{\Lambda_i \Lambda_s}} \right) - \sum_{k=i+1}^n m_k B_1^{ik} \left( \frac{q_i}{4\Lambda_i} - \frac{q_k}{4\sqrt{\Lambda_i \Lambda_k}} \right), \quad (3.3)$$

$$q'_i = \sum_{s=1}^{i-1} m_s B_1^{is} \left( \frac{p_i}{4\Lambda_i} - \frac{p_s}{4\sqrt{\Lambda_i \Lambda_s}} \right) + \sum_{k=i+1}^n m_k B_1^{ik} \left( \frac{p_i}{4\Lambda_i} - \frac{p_k}{4\sqrt{\Lambda_i \Lambda_k}} \right). \quad (3.4)$$

41 At the same time, the expressions  $\Pi_{ii}^{is}$ ,  $\Pi_{is}^{is}$ ,  $\Pi_{kk}^{ik}$ ,  $\Pi_{ik}^{ik}$  in equations (3.1) -(3.4) and  
 42 the Laplace coefficients retain their form, but they are already dimensionless quantities.  
 43 All notations are given in the article Prokopenya et al. (2022).

### 44 4. The evolutionary equations of the three-planet exosystem $K2 - 3$ 45 in explicit form

46 As an example, the case of  $n = 3$  was considered. The evolutionary equations (3.1)–  
 47 (3.4) for the  $K2 - 3$  exosystem are described by a system of 12 linear non-autonomous  
 48 differential equations, which are obtained explicitly. The resulting system splits into  
 49 two subsystems for eccentric and oblique elements. The resulting equations of secular  
 50 perturbations are difficult, so they will be investigated numerically.

### 51 5. Conclusion

52 The evolutionary equations of a multi-planetary problem with isotropically varying  
 53 masses at different rates in analogues of osculating Poincare elements were obtained.  
 54 These evolutionary equations can be used for any  $n$  planetary problem with variable  
 55 masses. The evolutionary equations for the  $K2 - 3$  exosystem were written explicitly.  
 56 The obtained evolutionary equations will be investigated numerically.

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