

## The 28th International Conference on Applications of Computer Algebra ACA'2023

# **PROGRAM & ABSTRACTS**

Warsaw University of Life Sciences – SGGW Institute of Information Technology July 17 - 21, 2023

WWW: https://aca2023.iit.sggw.pl

### **Program and Organizing Committees**

#### **General Chair**

Alexander Prokopenya, Warsaw University of Life Sciences - SGGW, Poland

#### Scientific Committee: ACA Working group

Gabriel Aguilera Venegas Alkiviadis Akritas Michel Beaudin Anouk Bergeron-Brlek Francisco Botana Bruno Buchberger Thierry Dana-Picard Victor Edneral Jose Luis Galan Garcia Victor Ganzha Mark Giesbrecht Hoon Hong David Jeffrey Erich Kaltofen Ilias Kotsireas (co-chair) Hiroshi Kai Robert H. Lewis Richard Liska Edgar Martinez-Moro Manfred Minimair Aleksandr Myllari Veronika Pillwein Alexander Prokopenya Louis-Xavier Proulx Pedro Rodriguez Cielos Tateaki Sasaki Yosuke Sato Werner Seiler Tony Shaska **Dimitris Simos** Margarita Spiridonova Stanly Steinberg Quoc-Nam Tran Elena Varbanova Nikolay Vasiliev Stephen Watt Michael Wester (co-chair) Wolfgang Windsteiger Zafeirakis Zafeirakopoulos

## Advisory Committee

Ilias Kotsireass, Waterloo, Canada Michael Wester, New Mexico, USA

## Local Organizing Committee

Ryszard Kozera (co-chair) Alexander Prokopenya (co-chair) Andrzej Zembrzuski Marcin Ziółkowski Artur Wiliński Włodzimierz Wojas Marcin Choiński Monika Krawiec Aleksandra Konopka Karol Struniawski Anna Dyniec Monika Hertel-Świerad Magdalena Magnuszewska Robert Budzyński Tomasz Minkowski

## Schedule for Computer Algebra Modeling in Science and Engineering Session

Organized by Alexander Prokopenya, Haiduke Sarafian

#### Tuesday, July 18

Build. 34, 3d floor, Room 3/40

14:00 – 14:30 **Ryszard Kozera** Fitting sparse reduced data 14:30 – 15:00 **Marcin Choinski** 

A discrete SIS model built on the strictly positive scheme

15:00 – 15:30 Marcin Ziółkowski On applications of computer algebra systems in queueing theory calculations

#### Wednesday, July 19

Build. 34, 3d floor, Room 3/40

14:00 - 14:30	Haiduke Sarafian Analyzing electric circuits with computer algebra
14:30 - 15:00	<b>Setsuo Takato</b> , Hideyo Makishita LMS with simple modeling developed by extended CindyJS and Maxima
15:00 - 15:30	Setsuo Takato, <b>Jose A. Vallejo</b> Billiards: At the intersection of Math, Physics and Computer Algebra
15:30 - 16:00	Coffee Break
16:00 - 16:30	Tatjana Petek, Valery G. Romanovski Computation of normal forms for systems with many parameters
16:30 - 17:00	Alina Ivashkevich, Victor Red'kov, <b>Alexander Chichurin</b> Spin 1 particle with anomalous magnetic moment in external uniform electric field: solutions with cylindric symmetry
17:00 - 17:30	<b>Alexander Prokopenya</b> On stability of stationary motion of the 3D swinging Atwood machine
17:30 - 18:00	<b>AmirHosein Sadeghimanesh</b> , Matthew England Semi-algebraic representations for the multistationarity region of reaction networks

#### Friday, July 21

Build. 34, 3d floor, Room 3/40

09:30 – 10:00 **Aigerim Ibraimova**, Alexander Prokopenya, Mukhtar Minglibayev Derivation of the evolution equations in the restricted three-body problem with variable masses by using Computer Algebra

#### Applications of Computer Algebra – ACA 2023 Warsaw, Poland, | July 17 – 21, 2023 Session on "*Computer Algebra Modeling in Science and Engineering*"

## Derivation of the evolution equations in the restricted three-body problem with variable masses by using Computer Algebra

#### Alexander Prokopenya<sup>1</sup>, Mukhtar Minglibayev<sup>2,3</sup> Aigerim Ibraimova<sup>2,3</sup>

[ibraimova@aphi.kz]

<sup>1</sup> Warsaw University of Life Sciences, Warsaw, Poland

<sup>2</sup> Al-Farabi Kazakh National University, Almaty, Kazakhstan

<sup>3</sup> Fesenkov Astrophysical Institute, Almaty, Kazakhstan

Observational astronomy states that celestial bodies are unsteady, their masses, sizes, shapes and structures change in the process of evolution. Variability in the masses of celestial bodies, especially at the nonstationary stage of the system, significantly affects the further dynamical evolution of this system as a whole [1, 2, 3]. In this connection, we consider the restricted three-body problem with variable mass in the presence of reactive forces. The problem was investigated by methods of perturbation theory, based on the aperiodic motion along a quasiconic section developed by us [4]. The system of differential equations of perturbed motion in oscillating variables of aperiodic motion along a quasi-conic section in the form of Newton's equation was derived [5]. By using Computer Algebra we obtained the equations of secular perturbation of the restricted three-body problem with variable masses in the presence of reactive forces [6].

#### Acknowledgments

This research is funded partially by the Science Committee of the Ministry of Science and Higher Education of the Republic of Kazakhstan (Grants No. AP14869472).

#### Keywords

restricted three-body problem, variable mass, reactive forces, secular perturbations

#### References

[1] T. OMAROV (ED.), *Non-Stationary Dynamical Problems in Astronomy*. Nova Science Publ., New-York, 2002.

[2] A. PROKOPENYA; M. MINGLIBAYEV; S. SHOMSHEKOVA, Computing Perturbations in the Two-Planetary Three-Body Problem with Masses Varying Non-isotropically at Different Rates. *Mathematics in Computer Science* **14**(2), 241–251 (2020).

[3] EGGLETON P. Evolutionary processes in binary and multiple stars. Cambridge University Press. – 2006. – P.332.

[4] M. MINGLIBAYEV, *Dynamics of gravitating bodies with variable masses and sizes*. LAMBERT Academic Publishing, Saarbrücken, 2012.

[5] M. MINGLIBAYEV; CH. OMAROV; A. IBRAIMOVA, New forms of the perturbed motion equation. *RNAS RK*. **2**(330), 5–13 (2020).

[6] IBRAIMOVA A.T., MINGLIBAYEV M.ZH., PROKOPENYA A.N. Study of Secular Perturbations in the Restricted Three-Body Problem of Variable Masses Using Computer Algebra // Computational Mathematics and Mathematical Physics. **63**(1), 115–125 (2023).