# Al-Farabi Kazakh National University, Kazakhstan Research Institute of Mathematics and Mechanics, Kazakhstan <br> Institute of Computational Mathematics and Mathematical Geophysics SB RAS, Russia <br> Novosibirsk State University, Russia Shanghai University of Finance and Economics, China Tianjin University of Finance and Economics, China Chinese Mathematical Society <br> hold an <br> International Conference <br> <br> INVERSE PROBLEMS IN <br> <br> INVERSE PROBLEMS IN <br> <br> FINANCE, Economics AND LIFE <br> <br> FINANCE, Economics AND LIFE SCIENCES 

 SCIENCES}

Almaty, Kazakhstan, December 26-28, 2017.

Content

# ON THE DIRECT AND INVERSE PROBLEM OF THE THEORY OF FILTRATION ON SPECIFICATION OF TECHNOLOGICAL INDICATORS 

Mukhambetzhanov S.T. ${ }^{1}$, Abdiakhmetova Z.M. ${ }^{2}$, Shazhdekeeva N.K. ${ }^{1}$

${ }^{1}$ Atyrau State University named after Kh.Dosmukhamedov; ${ }^{2}$ al Farabi Kazakh National University, Almaty
${ }^{2}$ zukhra.abdiakhmetova@gmail.com
The work is devoted to the investigation of the problem of pressure refinement in the areas of power supply and unloading and identification of technological indicators in the near-well zone of the formation. Concentration of transfer of individual components can be described by the equation of convective diffusion

$$
\begin{equation*}
m S_{r} \frac{\partial C_{r}}{\partial t}+\stackrel{\rho}{v_{r}} \nabla C_{r}-D_{r} \nabla^{2} C_{r}=0 \tag{1}
\end{equation*}
$$

$D_{r}$ - coefficient of dispersion, calculated by the formula

$$
\begin{equation*}
D_{r}=D_{0}\left[\frac{1}{F^{*} m}+0.5 \frac{\vec{U}_{r} d_{p} \sigma}{m D_{0}}\right]^{n} ; \stackrel{\rho}{U_{r}}=-\frac{K_{r}(x, y)}{\mu_{r}} \nabla P_{r} \tag{2}
\end{equation*}
$$

The filtration of a multicomponent mixture is described by a system of equations

$$
\begin{gather*}
\operatorname{div} \rho_{r} h \stackrel{\rho}{U}_{r}+m h S_{r} \frac{\partial \rho_{r}}{\partial t}+q_{r}=0  \tag{3}\\
\operatorname{div} \rho_{r} h C_{i} h \stackrel{\rho}{U_{r}}+m h S_{r} \frac{\partial \rho_{r} C_{i}}{\partial t}+q_{r} C_{i}=0 ; i=1, n ; \rho_{r}=\rho_{0} \frac{\rho_{r} T_{0}}{\rho_{0} T_{z}}  \tag{4}\\
\sum_{i=1}^{n} C_{i}=1 \tag{5}
\end{gather*}
$$

The initial conditions are

$$
\begin{equation*}
T=T_{0} ; p_{r}=p_{0}(x, y, t) ; C_{i}=C_{i 0}(x, y, t) ; i=i, n-1 \tag{6}
\end{equation*}
$$

The boundary conditions are as follows

$$
\begin{equation*}
F(x, y)=0 ; f\left(p_{r} \frac{\partial P_{r}}{\partial n}, x, y, t\right)=0 ; C_{i}=C_{i r}(x, y, t)=0 ; i=1, n-1 \tag{7}
\end{equation*}
$$

The direct problem of convective diffusion consists in finding functions $P_{r}$ and $C_{i}$, satisfying equations (4) - (5), the initial conditions, the boundary conditions. The functions $q_{r}(x, y, t)$, $k_{r}(x, y), m(x, y)$ and $h(x, y)$ are assumed to be given. The inverse problem for convective diffusion can be in determining the parameters $k_{r}, \mathrm{~m}$ and $h$ satisfying equations (4) - (11) if the data are known $P_{r}(x, y, t)$ and $C_{i}(x, y, t)$ in a certain part of the filtration area at certain points in time. Numerical experiments with real data were carried out.

