

Z. B. Rakisheva

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## THEORETICAL MECHANICS

*Educational manual*

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Educational manual was prepared on the base of a compulsory subject of theoretical mechanics, read by the authors for the students of specialty «Mechanics». It contains a lecture course of five modules, including kinematics, statics, dynamics of the mass point and the mechanical system, rigid body dynamics, analytical mechanics, as well as some of the tasks and exercises on these topics.

It will be of interest for students of specialties «Mathematics», «Mathematical and Computer Modeling» and others, which curriculum includes the study of theoretical mechanics.

Publishing in authorial release.

Учебное пособие подготовлено на основе обязательного курса теоретической механики, читаемого авторами для студентов специальности «Механика». Содержит курс лекций из пяти модулей, включающих кинематику, статику, динамику материальной точки и механической системы, динамику твердого тела, аналитическую механику, а также некоторые задачи и упражнения по этим темам.

Представляет интерес для студентов специальностей «Математика», «Математическое и компьютерное моделирование» и других, в учебный план которых входит изучение теоретической механики.

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CONTENT

LECTURE COURSE.....	6
Module I. KINEMATICS.....	6
Lecture 1. The subject of mechanics. Models of material bodies studied in mechanics. Basic concepts and laws of mechanics. Kinematics of a point. Problems of kinematic. Methods of the point's motion setting.....	6
Lecture 2. The speed and acceleration. The decomposition of the velocity and acceleration on the radial and transversal components. Decomposition of acceleration of the axes of the natural trihedral.....	10
Lecture 3. Mechanical system. The number of the freedom degrees of the system and a rigid body. Basic movements of a rigid body. Translational motion of a rigid body. Acceleration and velocity in the translational motion.....	15
Lecture 4. Rotational motion of a rigid body about a fixed axis. Angular velocity and the angular acceleration of a rigid body.....	17
Lecture 5. Plane-parallel motion of a rigid body. Velocities of the points of a plane figure. Instantaneous center of velocity.....	22
Lecture 6. Acceleration of the points of a plane figure. Instantaneous center of acceleration.....	26
Lecture 7. Compound motion of a point. Basic concepts. Full and relative derivatives of the vector. Addition of velocities. Theorem on the addition of accelerations (Coriolis theorem).....	30
Lecture 8. Complex motion of a solid body. The problem statement. Addition of the translational velocities. Addition of the instant angular velocities. Addition of the instant angular and translational velocities.....	36
Module II. STATICS.....	40
Lecture 9. Statics. Basic definitions and axioms of statics. Constraints. Constraint reactions. Axiom of constraints.....	40



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