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## **Heat and mass transfer processes at high-temperature media during combustion of low-grade pulverized coal**

**Abstract.** The article is devoted to the complex research processes of heat and mass transfer occurring in the real conditions of solid fuel (coal) combustion. Development of technological processes with economic and ecological advantages are the main purpose for many researches in thermal physics and technical physics. The complex processes of heat and mass transfer in the presence of combustion are non-stationary, strongly non-isothermal with a constant change in the physical and chemical state of the environment. It greatly complicates their experimental study. In this case, studying of heat and mass transfer in high-reacting media with simulation of physical and chemical processes occur during combustion of pulverized coal is important for the solution of modern power engineering industry and ecology problems. In this regard, a comprehensive study of heat and mass transfer processes at high-temperature media observed. Investigations based on the achievements of modern physics by using numerical methods for 3D modeling. Numerical experiments are conducted to describe and study aerodynamic characteristics, heat and mass transfer processes during the burning of pulverized Kazakhstan low-grade coal. The results obtained are of great practical importance, since they allow us to develop recommendations for the improvement and design of new combustion chambers and burners, and also can be useful in optimizing the whole process of burning fossil fuels.

**Keywords:** aerodynamic, combustion, heat exchange, numerical experiment

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## **Процессы тепломассопереноса в высокотемпературных областях при горении высокозольного пылеугольного топлива**

**Аннотация.** Статья посвящена комплексным исследованиям процессов тепломассопереноса, возникающие в реальных условиях горения твердого топлива (угля). Усовершенствование технологических процессов с экономическими и экологическими преимуществами является основной целью многих исследований в области теплофизики и теплоэнергетики. Комплексные процессы тепло- и массопереноса при наличии горения являются нестационарными, сильно неизотермическими с постоянным изменением физико-химического состояния окружающей среды. Это значительно усложняет их экспериментальное исследование. В этом случае изучение тепломассопереноса в высокореагирующих средах с моделированием физических и химических процессов происходящих при сжигании пылевидного угля имеет высокую важность для решения проблем современной энергетической промышленности и экологии. В связи с этим наблюдается всестороннее исследование процессов тепло- и массопереноса в высокотемпературных средах. Исследования основываются на достижениях современной физики с использованием численных методов 3D-моделирования. Численные эксперименты проводятся для описания и исследования аэродинамических характеристик, процессов тепломассопереноса при сжигании пылевидного казахстанского низкосортного угля. Полученные результаты имеют большое практическое значение, так как позволяют разрабатывать рекомендации по улучшению и проектированию новых камер сгорания и горелок, а также могут быть полезны при оптимизации всего процесса сжигания органического топлива.

**Ключевые слова:** аэродинамика, горение, теплообмен, численный эксперимент

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## **Күлділігі жоғары шаң-көмірлі отынның жануы кезіндегі жоғары температуралы аймақтарындағы жылу массатасымалдану процестері**

**Түйіндеме.** Мақала қатты отынның (көмірдің) жануының нақты жағдайларда туындайтын жылу және масса тасымалдану процестерін кешенді зерттеуге арналған. Экономикалық және экологиялық артықшылықтармен технологиялық үдерістерді жетілдіру жылу физикасы және жылу энергетикасы саласындағы көптеген зерттеулердің негізгі мақсаты болып табылады. Жану кезіндегі жылу мен масса

тасымалының кешенді процестері бейстационар, қоршаған ортаның физика-химиялық күйінің үздіксіз өзгеруімен изотермиялық емес болып келеді. Бұл олардың эксперименталды зерттеулерін қиындатады. Бұл жағдайда шаң тектес көмірді жағу кезінде орын алатын физикалық және химиялық процесстердің модельденуі арқылы жоғары реактивті орталардағы жылу мен масса тасымалын зерттеу қазіргі заманғы энергетика және экология проблемаларын шешу үшін өте маңызды болып табылады. Осыған байланысты, жоғары температуралы ортада жылу мен масса тасымалының процестерін жан-жақты зерттеу кең байқалады. Зерттеулер заманауи физиканың 3D модельдеудің сандық әдістерін қолдана отырып жасалған. Қазақстандағы төменгі сұрыпты көмірді жағу кезінде аэродинамикалық сипаттамаларды, жылу және масса тасымалдану процестерін сипаттау және зерттеу үшін сандық эксперименттер жүргізіледі. Алынған нәтижелер жоғары практикалық маңызға ие, өйткені олар жану камералары мен қыздырғыштарды жақсарту және жаңадан жобалау бойынша ұсыныстар әзірлеуге мүмкіндік береді, сондай-ақ органикалық отынының жану процесін оңтайландыруда пайдалы болып табылады.

**Кілт сөздер:** аэродинамика, жану, жылу алмасу, сандық эксперимент

## 1. Introduction

Solid fuel combustion is a complex physical and chemical phenomenon, which occurs at high temperatures with rapid and complete oxidation of combustible matter (carbon) by atmospheric oxygen and accompanied by a large amount of heat release [1-2]. Due to the low quality of main Kazakh coal deposits their exploitation at industry has increased scientific and applied relevance. Conducting of deep research on coal combustion in the real conditions can ensure the efficient technological process at all [3-5]. Heightened interest observed in particular to the study of heat and mass transfer processes at combustion of pulverized Kazakh coal with high ash content [6-10]. As it known combustion processes take place under conditions of strong turbulence and non-isothermal flow, multiphase medium with a significant impact of nonlinear effects of thermal radiation, interfacial interaction and multistage proceeding with chemical reactions [11-13]. Such phenomena have an important role in studying of the natural phenomenon of low-grade coal combustion. So investigations of turbulent chemically reacting media are extremely important to deepen knowledge of physical and chemical properties, for application possibilities.

In the context of depletion of natural energy resources and environmental pollution [12-13] rational use of energy fuel, increasing the efficiency of energy generation and solution of environmental problems are urgent and important task to solve. Development of technological processes with economic and ecological advantages are the main purpose for many researches in this area. The complex processes of heat and mass transfer in the presence of combustion are non-stationary, strongly non-isothermal with a constant change in the physical and chemical state of the environment. It greatly complicates their experimental study. In this case, studying of heat and mass transfer in high-reacting media with simulation of physical and chemical processes occur during combustion of pulverized coal is important for the solution of modern power engineering industry and ecology problems. In this regard, a comprehensive study of heat and mass transfer processes at high-temperature media observed. Investigations based on the achievements of modern physics by using numerical methods for 3D modeling [14-15] that in turn do not need labor force also much time. Applying of computational technology allow us to describe the actual physical processes that occur during combustion of energy fuel as accurate as possible [16-17]. Finally it has been put the objective of this paper oriented on holding numerical experiments on studying heat and mass transfer processes occurring in the areas of real geometry of the combustion chamber during the burning of energy fuel. It has been established mathematical model of physical-chemical combustion process.

## 2. Materials and methods

Study of processes of heat and mass transfer during coal combustion is possible only based on a complete theory of combustion physics. It includes a wide range of physical and chemical effects and its formulation of a mathematical model. For the simulation of heat and mass transfer in the presence of physical and chemical processes are used the fundamental laws of conservation of mass, momentum, energy [18-23]. Heat and mass transfer processes in the presence of physical and chemical transformations – is the interaction of turbulent flows. Therefore, the chemical processes here should take into account the law of conservation of components of the reacting mixture, multiphase medium, its turbulence degree, heat generation due to the radiation of heated fluid and chemical reactions. The law of conservation of substance written in the form of the law of conservation of matter as follows:

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} (\rho u_i) = q_N.$$

The law of conservation of momentum and the equation of motion expressed as:

$$\frac{\partial}{\partial t}(\rho u_i) = -\frac{\partial}{\partial x_j}(\rho u_i u_j) + \frac{\partial \tau_{ij}}{\partial x_j} - \frac{\partial P}{\partial x_i} + \rho f_i.$$

Law of energy conservation:

$$\frac{\partial}{\partial t}(\rho h) = -\frac{\partial}{\partial x_i}(\rho u_i h) - \frac{\partial q_i^{res}}{\partial x_j} + \frac{\partial P}{\partial t} + u_i \frac{\partial P}{\partial x_i} + \tau_{ij} \frac{\partial u_j}{\partial x_i} + S_h.$$

The conservation law for the components of the reaction mixture:

$$\frac{\partial}{\partial t}(\rho C_\beta) = -\frac{\partial}{\partial x_i}(\rho C_\beta u_i) + \frac{\partial j_i}{\partial x_i} + S_\beta.$$

For technical flames, it takes into account the transfer of matter only by diffusion. Transfer of substance due to the pressure gradient, the action of external forces (electric and magnetic fields) and thermal diffusion are small and they be neglected. Then the last equation written as follow:

$$\frac{\partial}{\partial t}(\rho C_\beta) = -\frac{\partial}{\partial x_i}(\rho C_\beta u_i) + \frac{\partial}{\partial x_i} \left( \frac{\mu_{eff}}{\sigma_{\beta eff}} \frac{\partial C_\beta}{\partial x_i} \right) + S_\beta.$$

In this paper for modeling of turbulence flows used the standard k-ε turbulence model, excluding the effect of lift or “twist” of flow, which is represented by the equation of turbulent kinetic energy transfer:

$$\frac{\partial(\overline{\rho k})}{\partial t} = -\frac{\partial(\overline{\rho u_j k})}{\partial x_j} + \frac{\partial}{\partial x_j} \left[ \frac{\mu_{eff}}{\sigma_k} \frac{\partial k}{\partial x_j} \right] + P - \overline{\rho} \cdot \varepsilon.$$

And the equation of dissipation (turbulent kinetic energy conversion into internal) turbulent kinetic energy ε:

$$\frac{\partial(\overline{\rho \varepsilon})}{\partial t} = -\frac{\partial(\overline{\rho u_j \varepsilon})}{\partial x_j} + \frac{\partial}{\partial x_j} \left[ \frac{\mu_{eff}}{\sigma_\varepsilon} \frac{\partial \varepsilon}{\partial x_j} \right] + C_{\varepsilon,1} \cdot \frac{\varepsilon}{k} \cdot P - C_{\varepsilon,2} \cdot \frac{\varepsilon^2}{k} \cdot \overline{\rho}.$$

Here the kinetic energy production:

$$P = \left[ \mu_{turb} \cdot \left( \frac{\partial \overline{u_i}}{\partial x_j} + \frac{\partial \overline{u_j}}{\partial x_i} \right) - \frac{2}{3} \cdot \rho \cdot k \cdot \delta_{ij} \right] \cdot \frac{\partial \overline{u_i}}{\partial x_j}.$$

And the rate of dissipation of turbulent energy:

$$\overline{\rho \varepsilon} = \mu_{turb} \cdot \frac{\partial u'_i}{\partial x_j} \cdot \left( \frac{\partial u'_i}{\partial x_j} + \frac{\partial u'_j}{\partial x_i} \right).$$

If  $k$  and  $\varepsilon$  are known, the turbulent viscosity determined by the Prandtl-Kolmogorov relationship as:  $\mu_{turb} = c \mu \rho \frac{k^2}{\varepsilon}$ .

Empirical constants  $c_\mu = 0.09$ ;  $\sigma_k = 1.00$ ;  $\sigma_\varepsilon = 1.30$ ;  $C_{\varepsilon 1} = 1.44$ ;  $C_{\varepsilon 2} = 1.92$  determined experimentally [18]. For the turbulent numbers of Prandtl and Schmidt were taken 0.9 [24].

A generalized equation of the transport value in a turbulent flow will then be:

$$\frac{\partial}{\partial t}(\rho\Phi) = -\frac{\partial}{\partial x_j}(\rho u_i \Phi) + \frac{\partial}{\partial x_j} \left[ \Gamma_{\phi, eff} \frac{\partial \Phi}{\partial x_j} \right] + S_\phi.$$

High-temperature media emits heat during combustion. As a result this thermal energy is transformed into radiant energy on the surface of the heated body. Thus, in the heat and mass transfer studies in the presence of combustion in the energy equation (i.e. heat transfer) should be considered the heat exchange by radiation too. On the heat exchange by radiation has a major influence of the water vapor and carbon dioxide. In modeling of flows heat exchange by radiation can be treated at temperatures  $500 \text{ K} < T < 2000 \text{ K}$  in the region of the visible and infrared parts of the spectrum. The emissivity of the gas mixture consists of components emissivity, and depends on the partial pressure, temperature and wavelength.

To determine the intensity of the radiation used the six-flow model in this study [25]. It allows approximating the intensity of the radiation with the help of the wall rows by the solid angle:

$$I = A_x(\vec{i}\Omega) + A_y(\vec{j}\Omega) + A_z(\vec{k}\Omega) + B_x(\vec{i}\Omega)^2 + B_y(\vec{j}\Omega)^2 + B_z(\vec{k}\Omega)^2 + \dots$$

This model has been used in the calculation of radiation heat transfer in combustion chambers and showed good agreement with the experimental data.

Physical and chemical processes occurring in the combustion chamber are rapid and complete processes of oxidation of the fuel (in this case high-ash content coal) take place at high temperatures, accompanied by a large release of energy due to chemical reactions and changes in the concentrations of all substances interact. To describe real physical transformations that occur during combustion of fuel, it is necessary to choose an adequate numerical model [26-27] of physical process. Chemical reactions, which in turn determines the source terms in the equations for energy and the substance components. In this paper adopted a chemical model, which takes into account only the key components of the reaction. A Mitchell-Tarbell model [28] is used, which takes into account the rank of coal for modeling nitrogen-containing components (in this case for the Kazakh coal ash content is 35.1%).

It was used one-step model of pyrolysis, when the change in the concentration of carbon described by the ordinary differential equation:

$$\frac{dc}{dt} = -k_{pyr}c,$$

$$k_{pyr} = k_{0pyr} T^n e^{-E_{pyr}/RT}.$$

The rate of combustion of volatiles  $\omega_{Vol}$  associated with the energy of turbulence  $k$  and its dissipation  $\varepsilon$ . For areas with a small amount of fuel and sufficient content of oxidizer, it have:

$$\omega_{1Vol} = C_1 \bar{c}_{Vol} \frac{\varepsilon}{k}.$$

For areas with sufficient amount of fuel reaction rate is determined by the stoichiometry coefficient  $\nu_{O_2Vol}$ :

$$\omega_{2Vol} = C_2 \frac{\bar{c}_{O_2} \varepsilon}{\nu_{O_2Vol} k}.$$

For areas with sufficient fuel and oxidant:

$$\omega_{3Vol} = C_{3Vol} \frac{\bar{c}_{CO_2} + \bar{c}_{H_2O} \varepsilon}{\nu_{O_2Vol} + 1} \frac{\varepsilon}{k}.$$

From these three speed, the minimum speed of volatile combustion in the actual process is established:

$$\omega_{Vol}^* = \min(\omega_{1Vol}, \omega_{2Vol}, \omega_{3Vol}).$$

where  $C_1 = 4.0$ ,  $C_2 = 4.0$ ,  $C_3 = 2.0$ .

The carbon C burning rate determined by the diffusion of oxygen into the pores of the solid particles and reactions on its surface:

$$k_C = \frac{k_C^{(D)} k_C^{(chem)}}{k_C^{(D)} + k_C^{(chem)}},$$

$$k_C^{(D)} = \frac{2\nu_c D M_c}{RT_m d_P}.$$

According to the Arrhenius law constant chemical reaction rate will be equal to:

$$k_C^{chem} = k_{0C} \exp(-E_C/RT).$$

The Mitchell-Tarbell model demonstrates the formation of nitrogen oxides NO<sub>x</sub> by the oxidation of fuel bound nitrogen. The kinetic scheme takes into account the reaction of the primary pyrolysis, homogeneous combustion of hydro carbonaceous compounds, heterogeneous combustion of coke and formation of nitrogen compounds by thermal and fuel NO<sub>x</sub> mechanisms. The last ending nitrogen centers considered in this model by subsystem of CN (HCN, CN et al.). The most important overall chemical reactions involved in NO<sub>x</sub> formation during coal combustion hypothesized to be those shown in Figure 1.

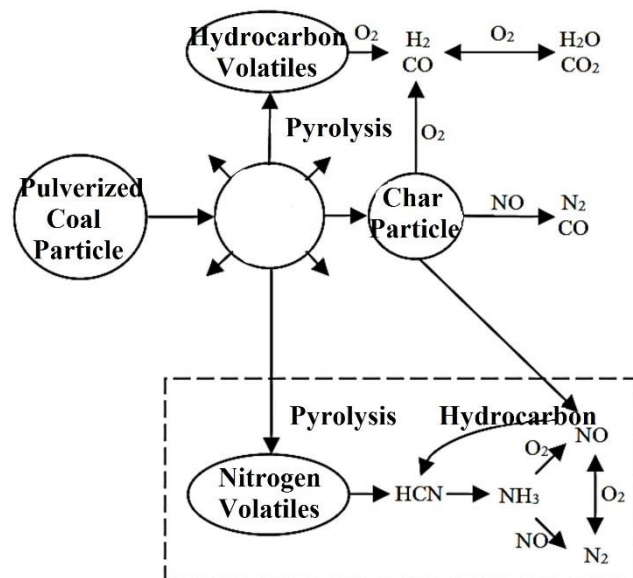


Fig. 1 – Schematic Mitchell-Tarbell kinetic model

To avoid mistakes that can lead to a physically meaningless result, an adequate initial and boundary conditions corresponding to real physical process given [29-30].

As an object of research were chosen the combustion process of Kazakh coal in combustion chamber of the real energy facility (boiler BKZ-75 of Shakhtinsk TEC in Kazakhstan). All conditions were taken into account of the real process of fuel combustion. For conducting numerical modeling were used control volume method, where in computational experiment the chamber has been divided into 126 496 cells.

### 3. Results of numerical modelling

Following shown results of three-dimensional modeling of heat and mass transfer processes during combustion of pulverized low-grade coal in real conditions of combustion chamber of boiler. Aerodynamic pattern of motion of two-phase turbulent flow of pulverized coal combustion causes the heat and mass transfer process in general. Figure 2 shows a two-dimensional graph of the full velocity vector, determined by the relationship:  $\vec{V} = \sqrt{U^2 + V^2 + W^2}$ . In the direction of camera output speed of flows decreased. The peak area values with maximum speed is clearly visible, which is equal to about 20 m/s. There at 4 meters by height of chamber located the combustor burners, and fed the fuel and oxidant mixture into the camera at maximum speed. Distribution character of flow velocity in height due to the vortex transfer of reacting medium and depending on the geometrical design of the chamber at all. At the outlet of chamber, it seen that velocity has a maximum value 8.76 m/s at section  $X=7.0$  m and an average value not exceeding the 5 m/s by height.

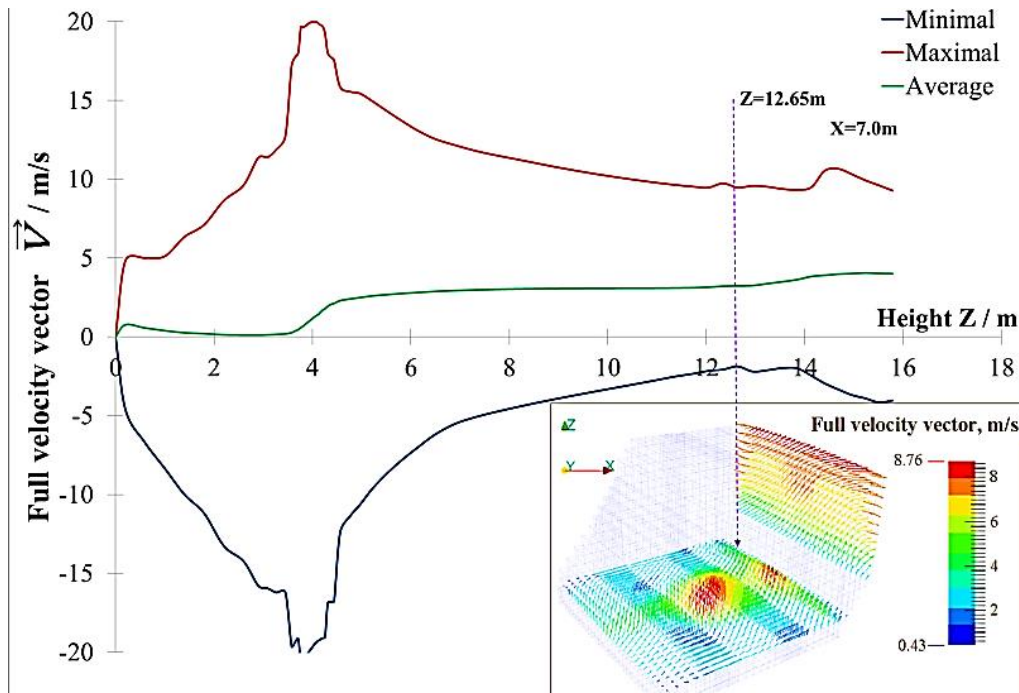


Fig. 2 – Distribution of full velocity vector

There is a maximum perturbation of the turbulence characteristics in the vortex region, which cause the biggest change of velocity (Figure 3). Available surroundings of vortical flow in the central region of the combustion chamber are beneficial to the process of burning pulverized coal (heat exchange and mass transfer).

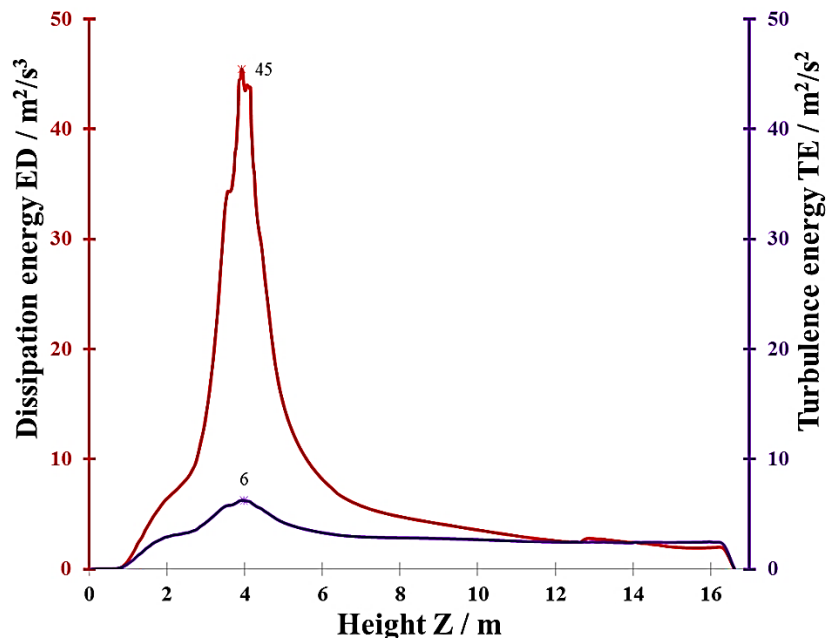


Fig. 3 – 2D distribution of turbulence characteristics

Figure 4 shows the distribution of maximum, minimum and average values of the temperature field in the combustion chamber. There is also observed a sharp decrease in the temperature of fuel feeding zone. This is because the fuel supplied by a lower temperature. It can be seen that temperature values reach their maximum values in the area below a girdle of the burners where located torch core (approximately at 3 meters). This is because in this area the eddy currents (from installed four burners: on 2 burners on two opposite tiers) have a maximum convective transfer that



increases the residence time of coal particles in here. As a result, in this area observed temperature rise to  $\sim 1370$  °C. In addition, at the output of the chamber maximum value of temperature is about 900-950 °C. This clearly seen from the 3D picture placed in the right corner of the figure. In the figure also presented the point of the theoretically calculated value of the temperature of exhaust gases in the output of the chamber defined according to the normative method of thermal calculation [31] and data from the natural experiments held in real TPP of RK [32].

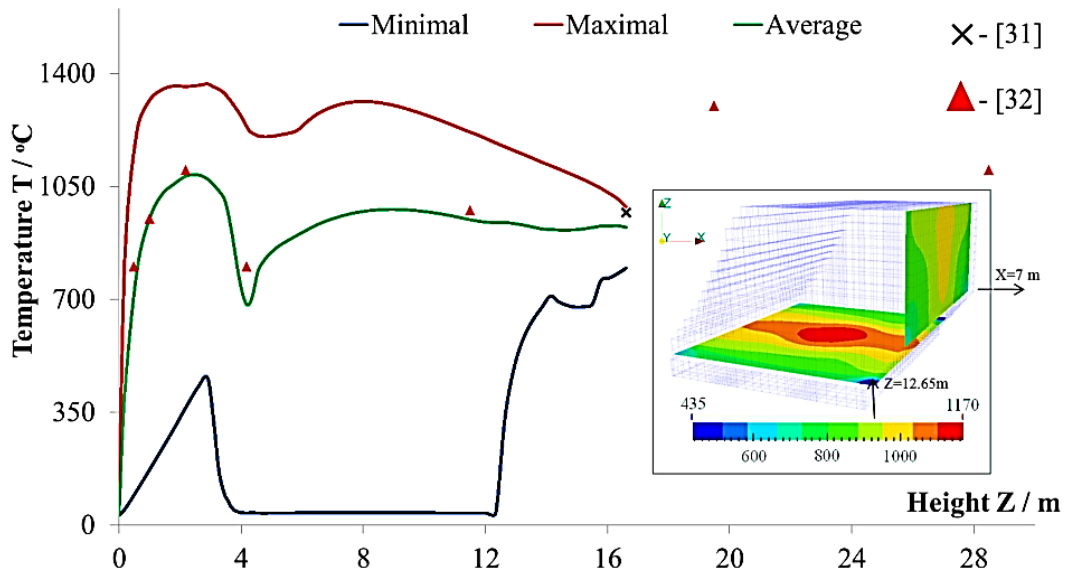


Fig. 4 – Distribution of temperature fields and its verification with known data

The method of thermal calculation in power engineering is still the most reliable for finding the temperature at the outlet of the combustion chamber. It is seen that the difference between the results of numerical calculation is small and is only 4.7%. This proves that the method of 3D modeling gives good description of real processes of heat and mass transfer of fuel combustion. The verification results show the good conformity with calculated results.

The following Figure 5, which shows the 3D temperature distribution by the chamber sections, observed the same character as in the previous Figure 4. Temperature values by the height of the combustion chamber monotonically fall. From 3D distribution it is seen that the core of flame is located in the lower part of chamber in the section  $Y=3.19$  m. Moreover, there the maximal value of temperature is equal to  $1340^{\circ}\text{C}$ . Temperature fields are decreased by the height of camera. So temperature has the value in average  $940^{\circ}\text{C}$  in section  $Z=12.65$  m, when it has  $922^{\circ}\text{C}$  at the section  $Z=7$  m (the output of chamber).

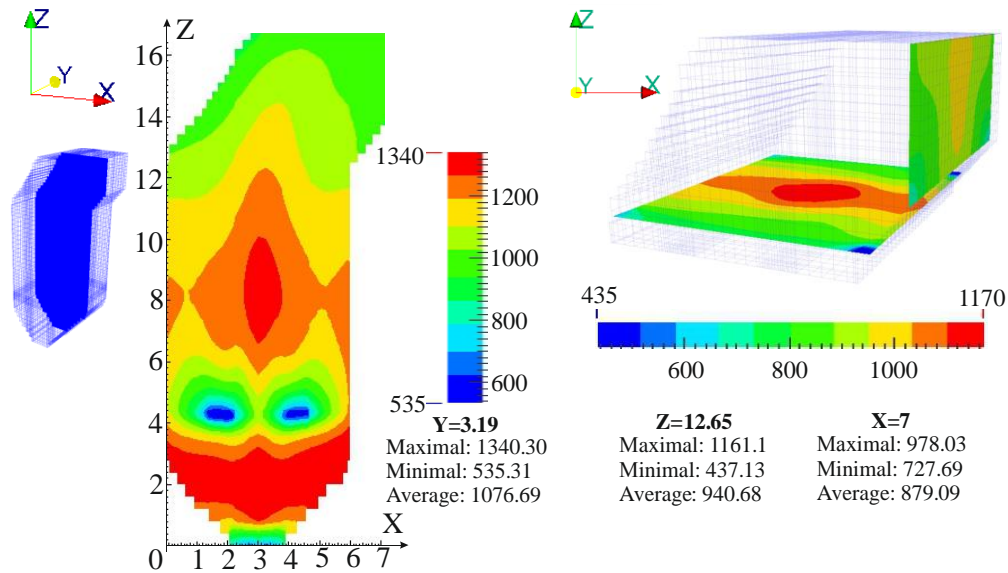


Fig. 5 – 3D temperature distribution by the chamber sections

Below shown the results of 3D modeling of carbon dioxide  $CO_2$  and nitrogen oxides  $NO_x$  concentration distributions. Carbon mono oxide  $CO$  reacts with oxygen completely and so formed its dioxide  $CO_2$ . Concentrations of carbon dioxide  $CO_2$  have their largest amount at the top areas of chamber (section  $Y=3.19$  m). And the minimal values are observed at the region, where the burner equipment is set. From the figure 6 at the section  $Y=3.19$  m it is seen that concentration of carbon dioxide  $CO_2$  has the minimal value equal to 0.0089 kg/kg. In addition, in average it raised to  $\sim 0.13$  kg/kg at the  $Z=12.65$  m section by height and  $\sim 0.15$  kg/kg at the outlet of the chamber (section  $X=7.0$  m).

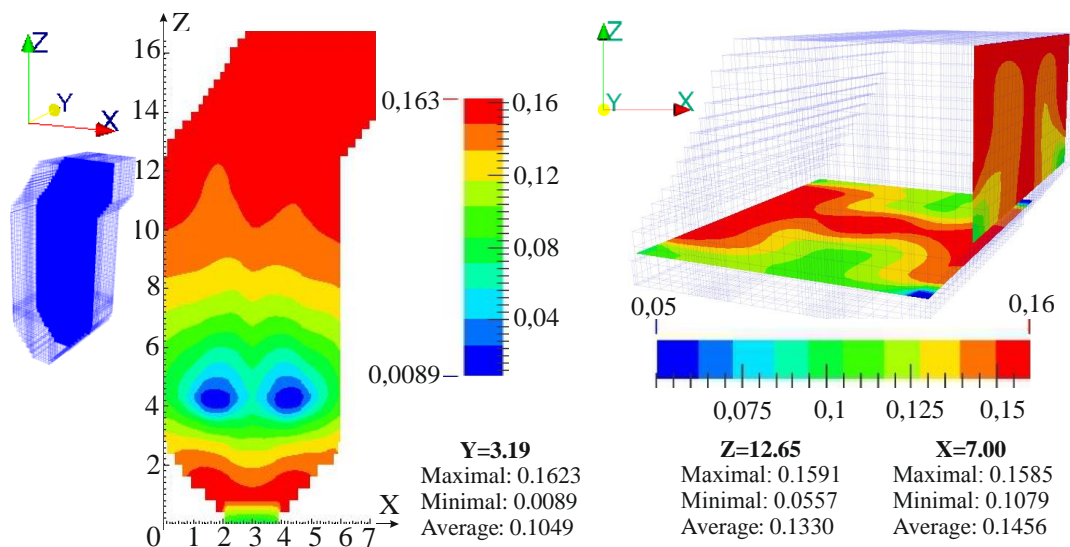


Fig. 6 – 3D distribution of the carbon dioxide concentrations on sections of the chamber ( $CO_2$ , kg/kg)

Nitrous oxides  $NO_x$  are formed by seven main nitrous compounds, but because of the small portions of them, except of nitrous mono-  $NO$  and dioxides  $NO_2$  (in total  $NO_x$ ), we negligible others. So it could be seen that the maximal amount of nitrous oxides  $NO_x$  concentrations 0.0109 kg/kg presented at the burners zone (Figure 7, section  $Y=3.19$  m). It caused with the fuel-N compound mechanism of  $NO_x$  formation. Where with height of boiler, it shown decreasing of nitrous oxides concentration. And it has the average value equal to  $5.09 \cdot 10^{-12}$  kg/kg at the output of the combustion volume (section  $X=7.0$  m).

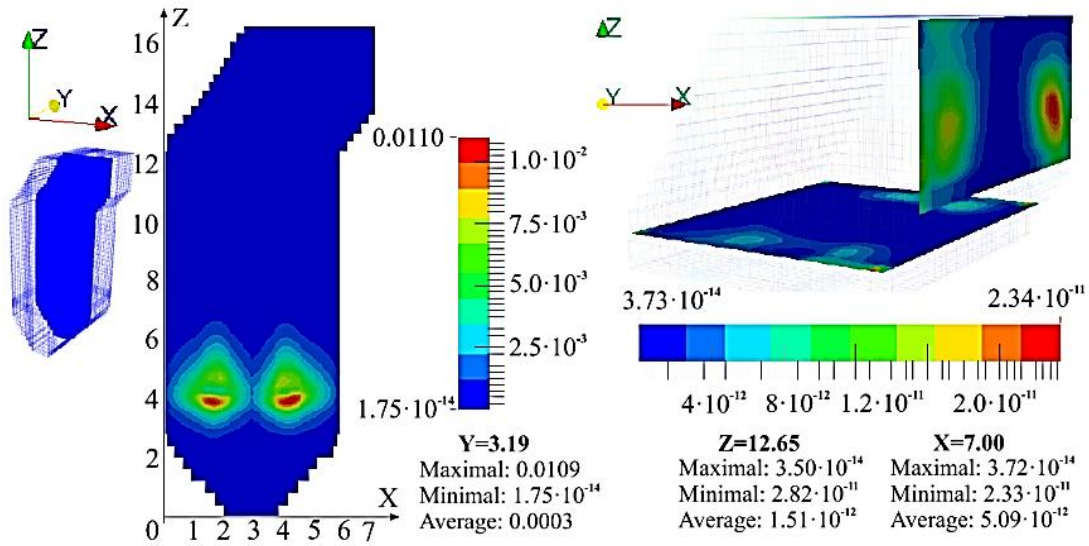


Fig. 7 – 3D distribution of the nitrogen oxides concentrations on sections of the chamber (NOx, kg/kg)

These concentration distributions of carbon dioxide and NOx verified with the known data as shown in Fig. 8.

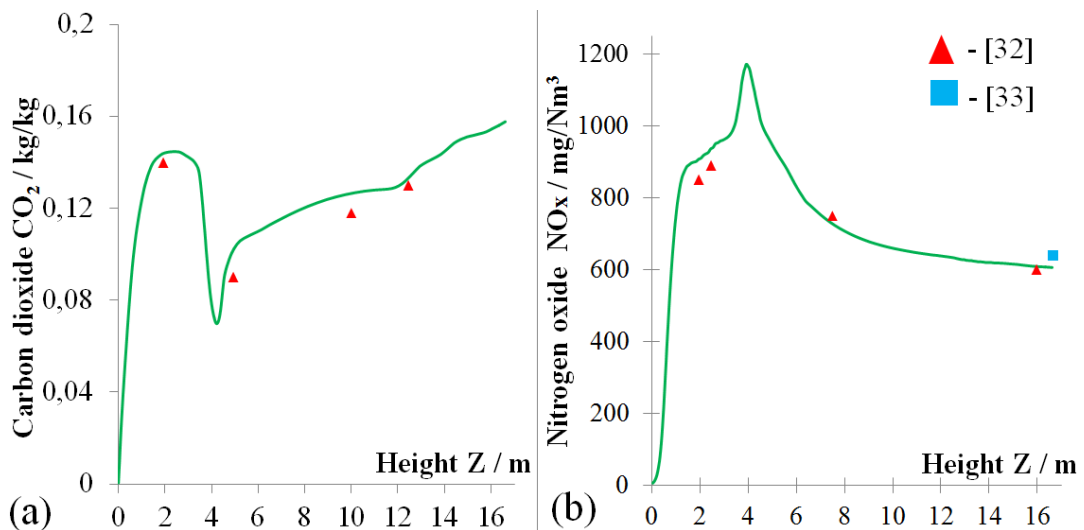


Fig. 8 – Verification of calculation results with known data [32, 33]

Concentrations of carbon dioxide CO<sub>2</sub> (a) and nitrogen oxides NOx (b) are in a good agreement with experimental data, received from real thermal power plant equipment [32]. Moreover nitrogen oxides NOx concentrations limit value for Kazakhstan Republic TPP's is given [33]. By comparisons of numerical experiment results held in this work with natural data from TPP, it noticed that the difference is for carbon dioxide CO<sub>2</sub> is 4 % and for nitrous oxides NOx is 5 %. So, considering results obtained in this paper we can propose the observed method of research of combustion processes is reliable and valid sufficiently to be useful in studying of low-grade coal combustion technological processes in energy objects.

#### 4. Conclusion and perspectives

In conclusion, with computational research of combustion and modelling of heat and mass transfer processes determined velocity characteristics of turbulent flows, their turbulent kinetic energy and dissipation energy. Aerodynamic characteristics shows that intensive mixing of fuel and

oxidant held in the central part of the chamber. In addition, it caused the increasing of temperature values to 1370°C in core of torch and monotonically decreased to 922°C at the outlet. Formation of hazardous substances as carbon and nitrous oxides (CO<sub>2</sub>, NO<sub>x</sub>) are depends on their chemical interaction with oxygen. Carbon dioxide has its maximal values at the outlet of the chamber (~ 0.16 kg/kg), and the nitrous oxides have the maximal amount of ~ 1200 mg/Nm<sup>3</sup> at the burners' zone. Obtained results of numerical experiments have great theoretical and practical importance, as it will allow improve the design of combustion chambers and burners, to optimize the process of burning of high-ash content energy coal of Kazakhstan Republic.

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### References:

1. Williams F. Combustion theory. - California: Westview Press, 1985. – 704 p.
2. Zarrouk S.J., O'Sullivan M.J., St George J.D. Combustion Theory and Modelling. – 2006. – 907 p.
3. Messerle V. E., Ustimenko A. B., Askarova A.S., Nagibin A.O. Pulverized coal torch combustion in a furnace with plasma-coal system // Thermophysics and aeromechanics. – 2010. – Vol. 17, issue 3. – P. 435-444.
4. Askarova A.S., Messerle V. E., Ustimenko A. B., Bolegenova S. A., Maksimov, V. Yu. Numerical simulation of the coal combustion process initiated by a plasma source // Th. and aeromechanics. – 2014. – V. 21, is. 6. – P. 747-754.
5. Karpenko E.I., Askarova A.S., Messerle V. E., Ustimenko A. B. Mathematical modelling of the processes of solid fuel ignition and combustion at combustors of the power boilers // 7th International Fall Seminar on Propellants, Explosives and Pyrotechnics. – Xian, 2007. – Vol. 7. – P. 672-683.
6. Karpenko E.I., Messerle V.E., et al. Plasma enhancement of combustion of solid fuels // Journal of High Energy Chemistry. – Vol. 40, Issue: 2, 2006. – P. 111-118.
7. Askarova A., Buchmann M. A Structure of the flame of fluidized-bed burners and combustion processes of high-ash coal//Gesell Energietechn., Combustion and incineration - eighteenth dutch-german conference on flames, VDI Berichte. – 1997. – V. 1313. – P. 241-244.
8. Askarova A., Bolegenova S., Safarik P., Maximov V., Beketayeva M. Numerical Modeling of Pulverized Coal Combustion at Thermal Power Plant Boilers // Journal of thermal science. – 2015. – Vol. 24, issue 3. – P. 275-282.
9. Askarova, A.S., Lavrichsheva, Ye.I., Leithner, R., Müller, H., Magda, A. Combustion of low-rank coals in furnaces of Kazakhstan coal-firing power plants // VDI Berichte. – 2007. – Issue 1988. – P. 497-502.
10. Askarova A.S., Karpenko E.I., Messerle V.E., Ustimenko A.B., Loktiomova I.V. Optimization of the combustion of power station coals using plasma technologies // Thermal Engineering. – 2004. - V. 51, Iss. 6, P. 488-493.
11. Law Ch. K. Combustion Physics. – Cambridge: Cambridge University Press, 2006. – 742 p.
12. Askarova A., Bolegenova S., Maximov V., Bekmukhamet A., Beketayeva M.T., Gabitova Z. Control of harmful emissions concentration into the atmosphere of megacities of Kazakhstan Republic // 2014 International Conference on Future Information Engineering. – Beijing, China, 2014. – IERI Procedia. – Vol. 10. – P. 252–258.
13. Askarova A.S., Bolegenova S.A., Maximov V. Ju., Bekmukhamet A., Beketayeva M.T. Analysis of formation harmful substances formed as a result of burning the low-grade coal in the combustion chamber of the industrial boiler of Kazakhstan using CFD-code FLOREAN // 17th Conference on Process Integration, Modelling and Optimisation for Energy Saving and Pollution Reduction (PRES 2014). – Prague, Czech Republic, August 23-27, 2014. – P. 7.160.
14. Askarova A., Bekmukhamet A., Bolegenova S., Ospanova S., Bolegenova S., Maximov V., Beketayeva M., Ergalieva A. 3-D Modeling of Heat and Mass Transfer during Combustion of Solid Fuel in Bkz-420-140-7C Combustion Chamber of Kazakhstan // Journal of Applied Fluid Mechanics. - 2016. - Vol.9, №2. - P. 699-709.
15. Xu Wen, Kun Luo Analysis of pulverized coal flame stabilized in a 3D laminar counterflow // Combustion and Flame. – 2018. – V. 189. – P. 106–125.
16. Askarova A., Messerle V., Ustimenko A., Bolegenova, S., etc. Reduction of noxious substance emissions at the pulverized fuel combustion in the combustor of the BKZ-160 boiler of the Almaty heat electropower station using the “Overfire Air” technology // Thermophysics and aeromechanics. – 2016. – Vol. 23, issue 1. – P. 125-134.
17. Askarova A. S., Bolegenova S.A., Maximov V.Y., Bekmukhamet A, Beketayeva M.T. Gabitova Z.K., etc. Computational method for investigation of solid fuel combustion in combustion chambers of a heat power plant // High temperature. – 2015. – Vol. 5, issue 5. – P. 751-757.
18. Muller H. Numerische Simulation von Feuerungen. – Braunschweig: IWBT, 1997. – P. 8. (in German)
19. Leithner R., Müller H. CFD Studies for Boilers // Second M.I.T. Conference on Computational Fluid and Solid Mechanics. – Cambridge, 2003. – 172 p.
20. Askarova A.S., Bolegenova S.A., Bolegenova S., Bekmukhamet A., Maximov V.Yu., Beketayeva M.T. Numerical experimenting of combustion in the real boiler of CHP // International Journal of Mechanics. – ISSN: 1998-4448. – Issue 3. – Volume 7, 2013. – P. 343-352.

21. Askarova A.S., Heierle E.I., Manatbayev R., etc. CFD study of harmful substances production in coal-fired power plant of Kazakhstan // Bulgarian Chemical Communications. – 2016. – Vol. 48. – Special Issue E. – P. 260-265.
22. Launder B., Spalding D. The numerical computation of turbulent flows // Comp. Meths. Appl. Mech. Eng. – 1974. – V.3. – P. 269–289.
23. El-Mahallawy L., El-Din Habik S. Fundamentals and technology of combustion. – Oxford: Elsevier Science: Energy, 2002. – 839 p.
24. Askarova A.S., Messerle V.E., Ustimenko A.B., Loktiomova I.V. 3D Modeling of the Two-Stage Combustion of Ekibastuz Coal in the Furnace Chamber of a PK-39 Boiler at the Ermakovo District Power Station // Thermal Engineering. – 2003. – V. 50, Issue 8. – P. 633-638.
25. De Marco A., Lockwood F. A new flux model for the calculation of radiation furnaces // Italian Flame Days. – 1975. – P. 1-13.
26. Leithner R., Askarova A., Bolegenova S., Bolegenova S., Maximov V., Ospanova S., Ergalieva A., Nugymanova A., Beketayeva M. Computational modeling of heat and mass transfer processes in combustion chamber at power plant of Kazakhstan // 20th International Conference on Circuits, Systems, Communications and Computers (CSCC). – July 14-17, Corfu, Greece. – 2016. – P. 5.
27. Askarova A., Vockrodt S., Leithner R. et al. Firing technique measures for increased efficiency and minimization of toxic emissions in Kasakh coal firing // VDI, 19th German Conference on Flames, Germany, VDI Gesell Energietechn; Verein Deutsch Ing., Combustion And Incineration, VDI Berichte. – 1999. – V. 1492. – 93 p.
28. Mitchell J.W., Tarbell J.M. A kinetic model of nitric oxide formation during pulverized coal combustion // AIChE Journal. – 1982. – V. 28. – P. 302-320.
29. Askarova A., Bolegenova S. et al. Influence of boundary conditions to heat and mass transfer processes // Intern. Journal of Mechanics. - 2016. - Vol.10. - P. 320-325.
30. Askarova A.S., Bolegenova S.A., Bolegenova S.A., Maximov V., Beketayeva M.T., Shortanbayeva Zh.K. On the effect of the temperature boundary conditions on the walls for the processes of heat and mass transfer // International journal of mechanics. - 2016. - Vol.10. - P. 349-355.
31. Teplovoi raschet kotlov: Normativnyi metod. – SPb.: NPO CKTI, 1998. – 256 p. (in Russian)
32. Aliyarov B. K., Aliyarova M. B. Szhiganiye kazakhstanskikh ugley na TES i na krupnykh kotelnykh: opyt i perspektivy. – Almaty: Gylym ordasy, 2011. – 304 p. (in Russian).
33. RND 34.02.303-91 Otrasleyaya instruktsiya po normirovaniyu vrednykh vybrosov v atmosferu dlya teplovykh elektrostantsiy i kotel'nykh. – Astana: MOOS RK, 2004. (in Russian)